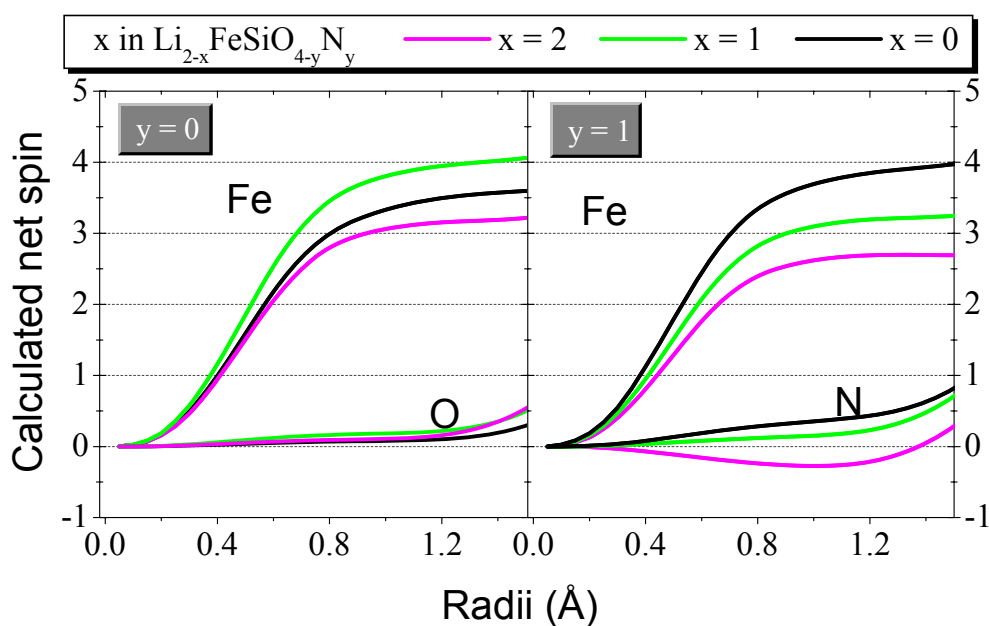
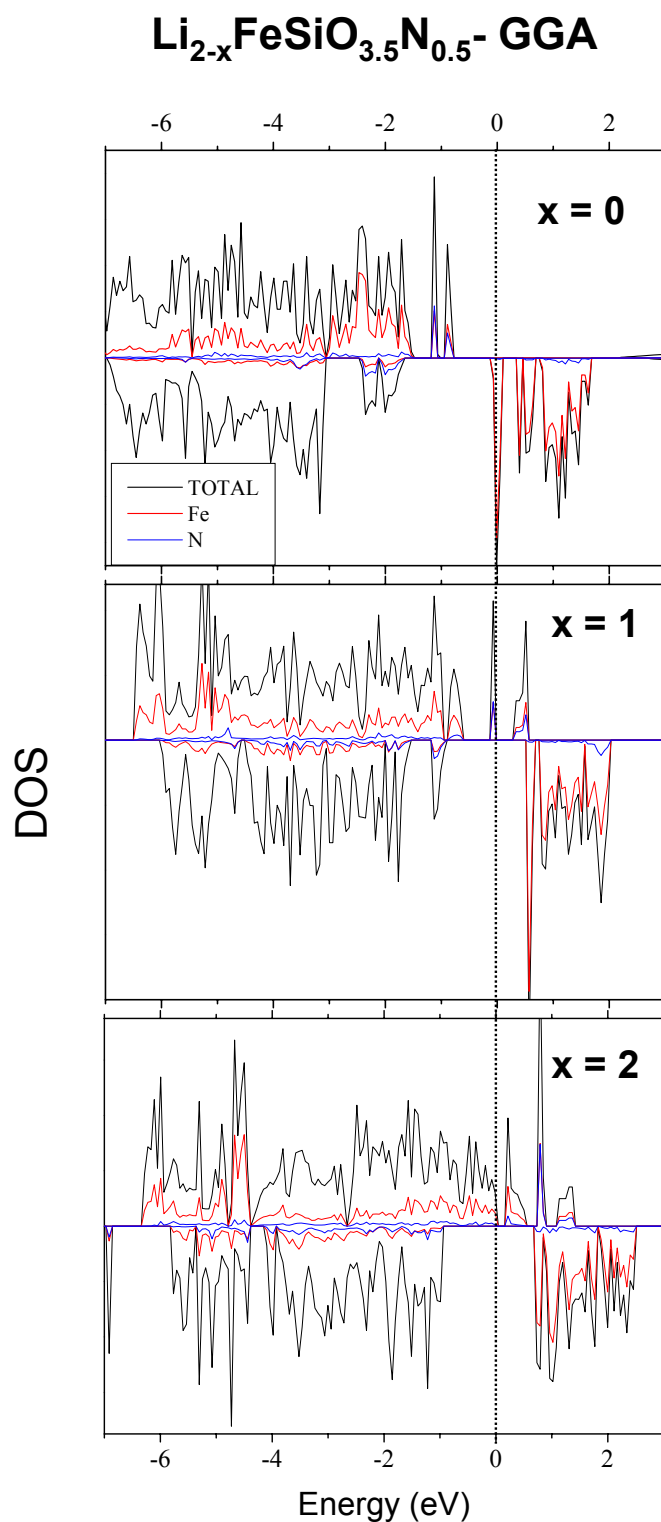


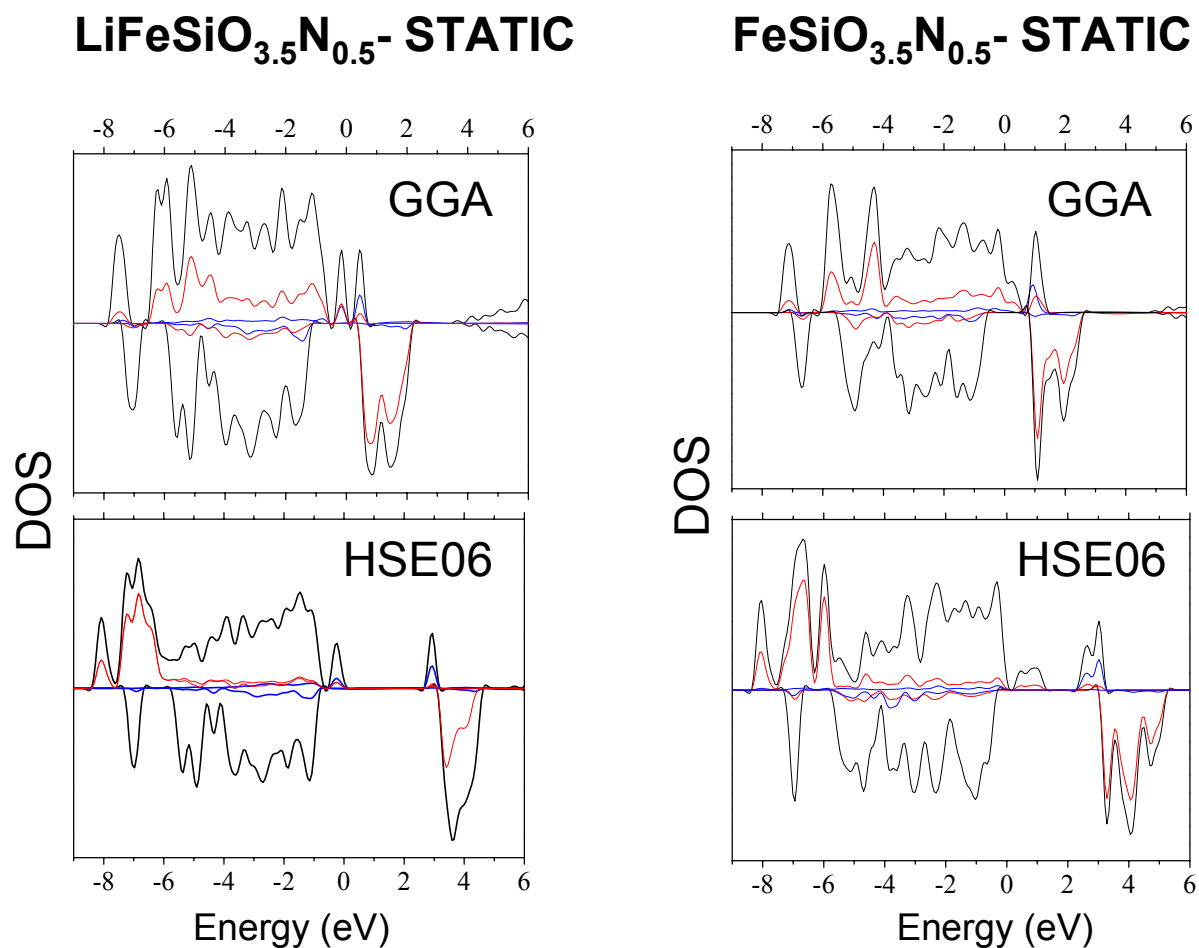
SUPPLEMENTARY INFORMATION



Conventional relaxed GGA calculations.- Integrated net spin as a function of the radius around N (O), and Fe centres in the ground states of the $\text{Li}_{2-x}\text{FeSiO}_{4-y}\text{N}_y$. Left panel $\text{Li}_2\text{FeSiO}_4$ ($y=0$) and right panel $\text{Li}_2\text{FeSiO}_3\text{N}$ ($y=1$). The lithium content (x) is represented in black ($x=0$), green ($x=1$) and pink ($x=2$). To be compared with figure 5 in the manuscript.



Conventional relaxed GGA calculations.- Calculated density of states (DOS) of the ground states of the $\text{Li}_{2-x}\text{FeSiO}_{3.5}\text{N}_{0.5}$ for $x = 0, 1$ and 2 . The black lines denote the total DOS; the partial DOS of Fe and N are represented in red and blue, respectively. The zero of the energy has been set at the Fermi level. To be compared with the middle column of figure 7 in the manuscript.



Hybrid Functional calculations.- Calculated density of states (DOS) of the ground states of $\text{LiFeSiO}_{3.5}\text{N}_{0.5}$ and $\text{FeSiO}_{3.5}\text{N}_{0.5}$ within the conventional GGA and the HSE06 hybrid functional. These static calculations were performed for the optimized structures of the relaxed-GGA+U calculations. The black lines denote the total DOS; the partial DOS of Fe and N are represented in red and blue, respectively. The zero of the energy has been set at the Fermi level.