

# **Ultrasensitive Sorption Behavior of Isostructural Lanthanide-Organic Frameworks Induced by Lanthanide Contraction**

Zhongjun Lin <sup>a</sup>, Ruqiang Zou <sup>a,\*</sup>, Wei Xia <sup>a</sup>, Liangjie Chen <sup>a</sup>, Xidong Wang <sup>a</sup>, Fuhui Liao <sup>b</sup>, Yingxia Wang <sup>b</sup>, Jianhua Lin <sup>b</sup>, Anthony K. Burrell <sup>c</sup>

<sup>a</sup> *College of Engineering, Peking University, Beijing 100871, China. E-mail: rzou@pku.edu.cn.* <sup>b</sup> *College of Chemistry and Molecule Engineering, Peking University, Beijing 100871, China.* <sup>c</sup> *Chemical Sciences and Engineering Division, Argonne National Laboratory, 9700 S. Cass Avenue, Argonne, IL 60439.*

**Table S1.** Crystallographic Data and Structural Refinement Summary for **Pr-LOF**.

Formula	PrC <sub>33</sub> H <sub>33</sub> N <sub>2</sub> O <sub>10</sub>
Molecular weight	758.52
T (K)	293(2)
Crystal system	hexagonal
space group	<i>P</i> 6 <sub>1</sub> 22
<i>a</i> (Å)	16.4393(3)
<i>b</i> (Å)	16.4393(3)
<i>c</i> (Å)	23.7770(9)
Volume (Å <sup>3</sup> )	5564.9(3)
$\alpha$ (deg)	90
$\beta$ (deg)	90
$\gamma$ (deg)	120
<i>Z</i>	6
$\rho$ (g/m <sup>3</sup> )	1.32559
R1, wR2 [ <i>I</i> >2 $\sigma$ ( <i>I</i> )]	0.0486, 0.1455

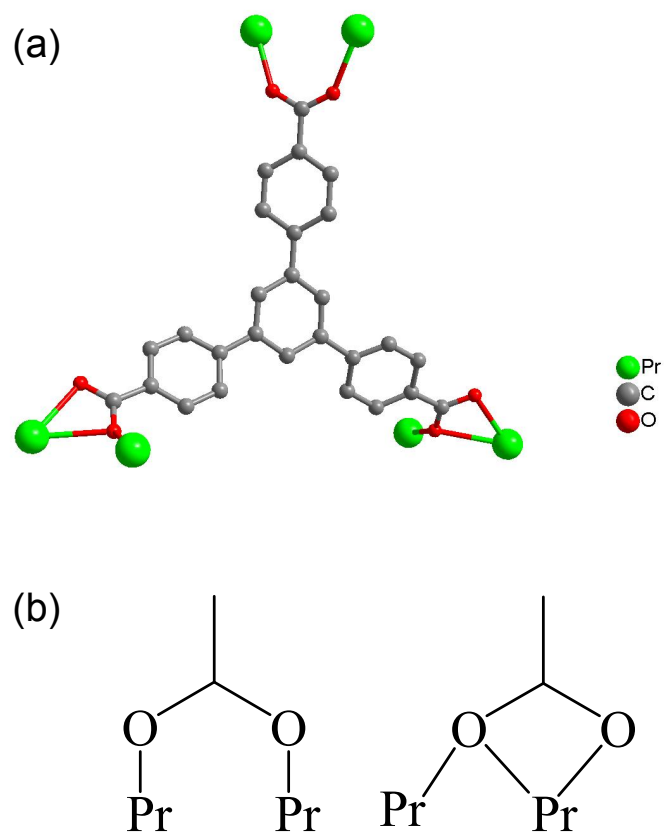
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$R_1 = \frac{\sum ||F_o| - |F_c||}{\sum |F_o|}$ .  $wR_2 = [\frac{\sum w(F_o^2 - F_c^2)^2}{\sum w(F_o^2)^2}]^{1/2}$ .

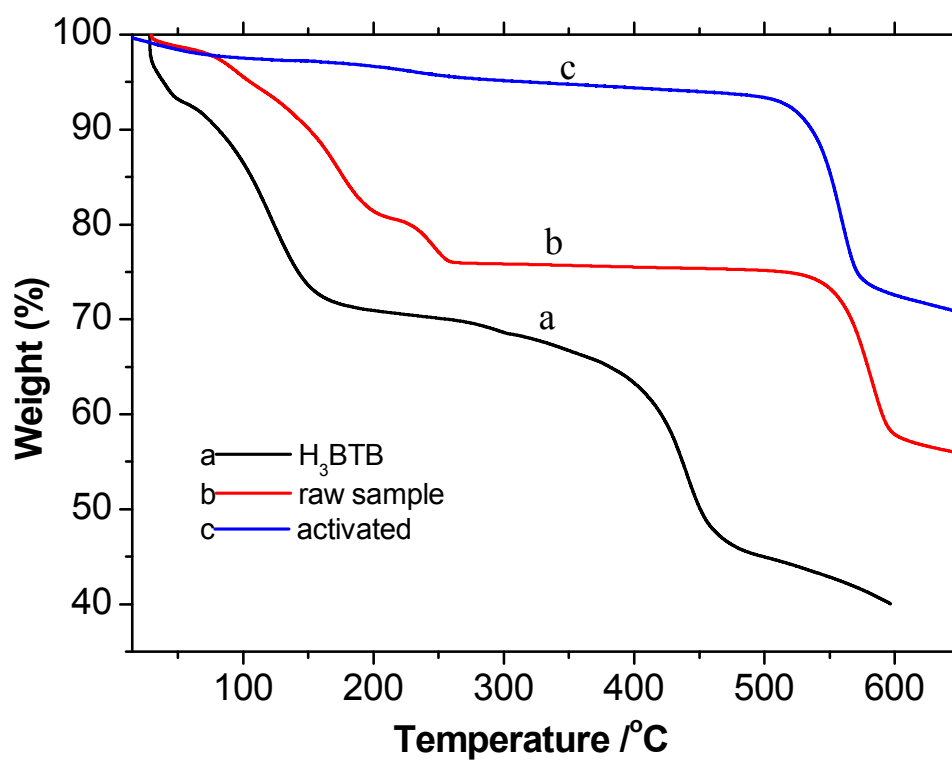
**Table S2.** Selected bond lengths (Å) and angles (°) of complex **Pr-LOF**.

Pr(1)-O(3)#1	2.371(5)	Pr(1)-O(2)#5	2.505(6)
Pr(1)-O(3)#2	2.371(5)	Pr(1)-O(1W)	2.478(9)
Pr(1)-O(2)#3	2.468(5)	Pr(1)-O(1)	2.707(5)
Pr(1)-O(2)#4	2.468(5)	Pr(1)-O(2)	2.505(6)
Pr(1)-O(1)#5	2.707(5)		
O(3)#1-Pr(1)-O(3)#2	76.5(3)	O(1)#4-Pr(1)-O(2)	95.5(3)
O(3)#1-Pr(1)-O(1)#3	136.1(2)	O(1W)-Pr(1)-O(2)	74.43(17)
O(3)#2-Pr(1)-O(1)#3	72.92(19)	O(2)#5-Pr(1)-O(2)	148.9(3)
O(3)#1-Pr(1)-O(1)#4	72.92(19)	O(3)#1-Pr(1)-O(1)#5	74.65(17)
O(3)#2-Pr(1)-O(1)#4	136.1(2)	O(3)#2-Pr(1)-O(1)#5	79.65(18)
O(1)#3-Pr(1)-O(1)#4	148.5(2)	O(1)#3-Pr(1)-O(1)#5	69.46(19)
O(3)#1-Pr(1)-O(1W)	141.74(16)	O(1)#4-Pr(1)-O(1)#5	120.30(16)
O(3)#2-Pr(1)-O(1W)	141.74(17)	O(1W)-Pr(1)-O(1)#5	106.43(12)
O(1)#3-Pr(1)-O(1W)	74.24(12)	O(2)#5-Pr(1)-O(1)#5	49.38(19)
O(1)#4-Pr(1)-O(1W)	74.24(12)	O(2)-Pr(1)-O(1)#5	143.4(3)
O(3)#1-Pr(1)-O(2)#5	79.0(3)	O(3)#1-Pr(1)-O(1)	79.65(18)
O(3)#2-Pr(1)-O(2)#5	127.7(2)	O(3)#2-Pr(1)-O(1)	74.65(17)
O(1)#3-Pr(1)-O(2)#5	95.5(3)	O(1)#3-Pr(1)-O(1)	120.30(16)
O(1)#4-Pr(1)-O(2)#5	76.0(2)	O(1)#4-Pr(1)-O(1)	69.46(19)
O(1W)-Pr(1)-O(2)#5	74.43(17)	O(1W)-Pr(1)-O(1)	106.43(12)
O(3)#1-Pr(1)-O(2)	127.7(2)	O(2)#5-Pr(1)-O(1)	143.4(3)
O(3)#2-Pr(1)-O(2)	79.0(3)	O(2)-Pr(1)-O(1)	49.38(19)
O(1)#3-Pr(1)-O(2)	76.0(2)	O(1)#5-Pr(1)-O(1)	147.1(2)

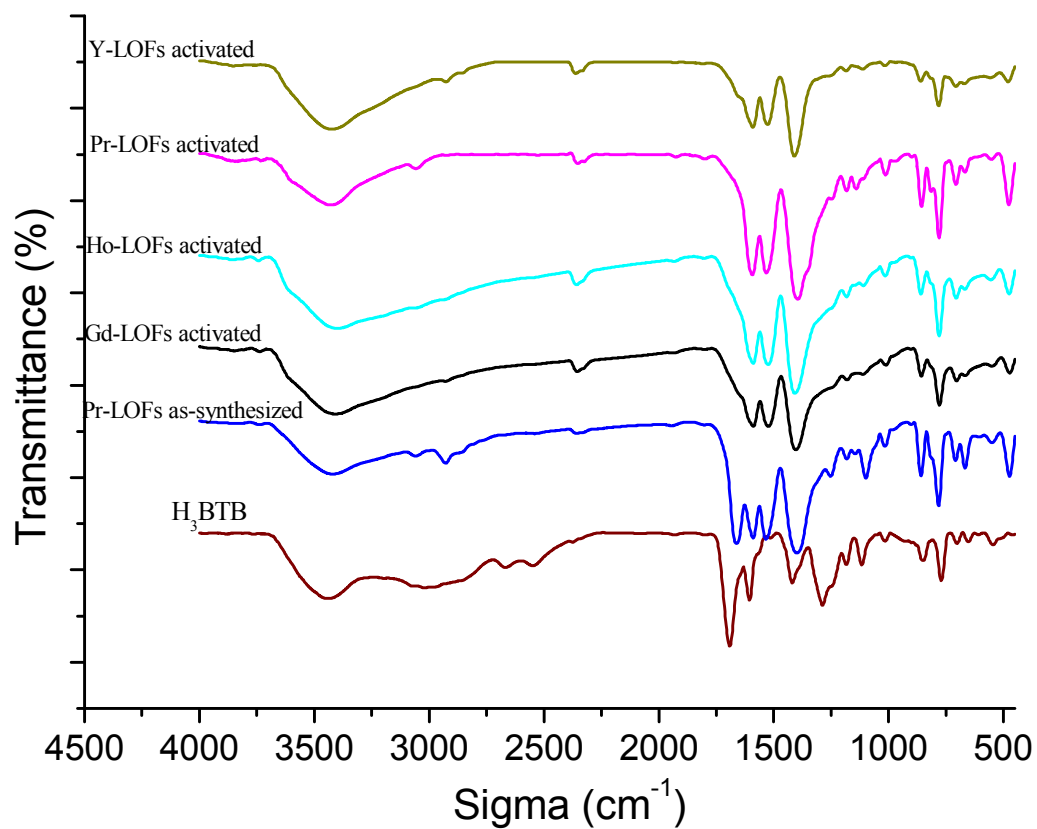
<sup>a</sup> Symmetry transformations used to generate equivalent atoms: #1  $x+1, y+1, z$ ; #2  $x-y+1, -y+1, -z$ ; #3  $y, -x+y+1, z-1/6$ ; #4  $x, x-y+1, -z+1/6$ ; #5  $x-y+1, -y+2, -z$ ; #6  $x, x-y, -z+1/6$ ; #7  $x-y+1, x, z+1/6$ ; #8  $x-1, y-1, z$ .



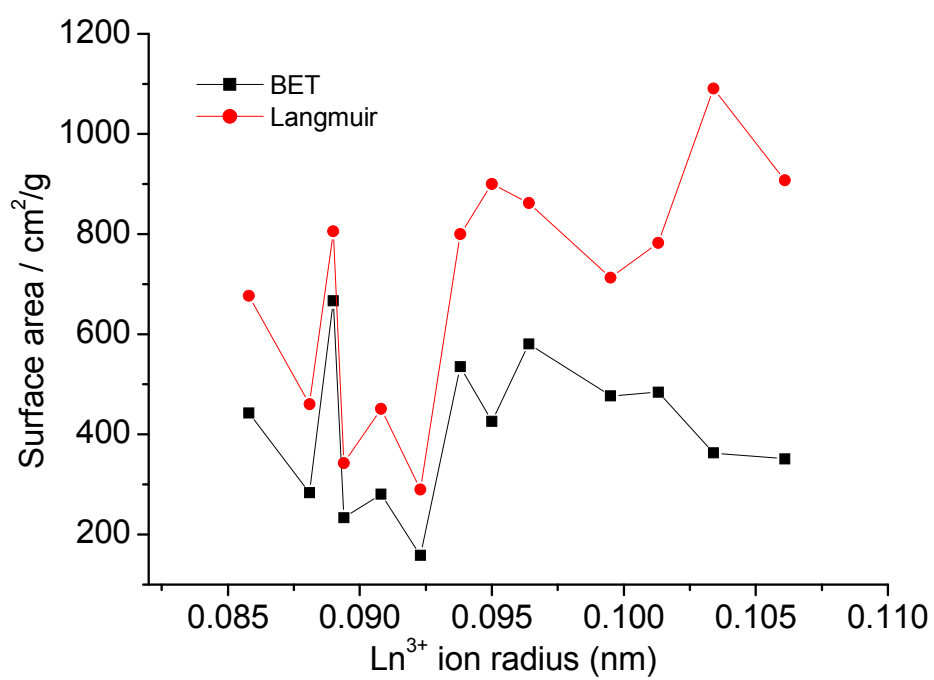
**Figure S1.** (a) The coordination environment of BTB ligand. (b) The two types of binding modes of BTB ligand.



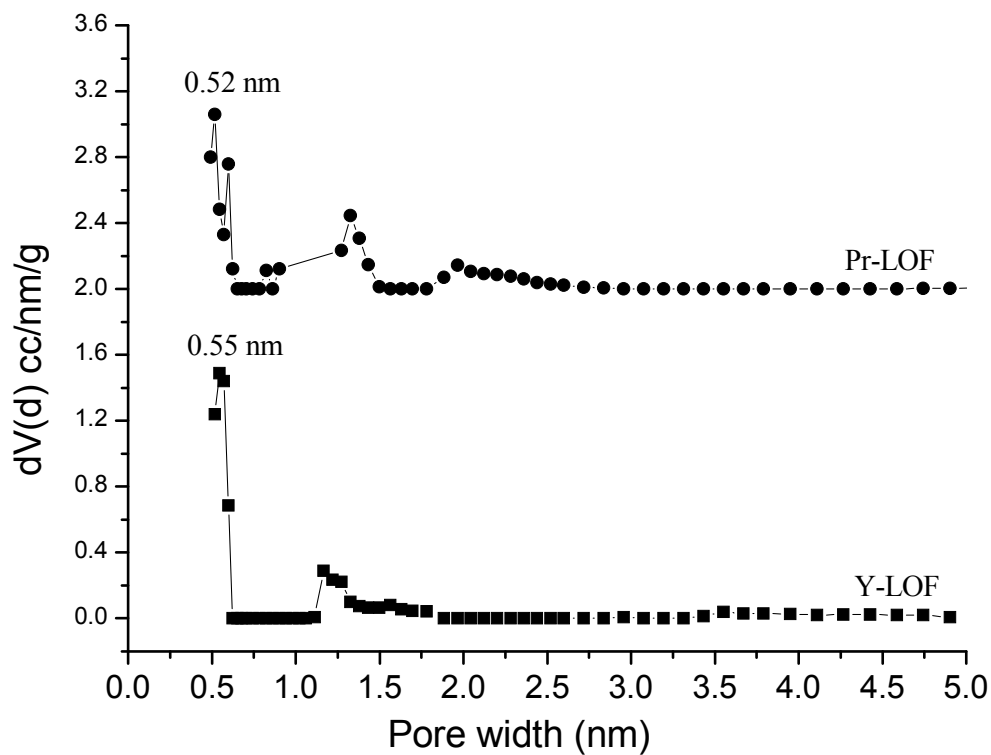
**Figure S2.** TG curves of H<sub>3</sub>BTB, raw sample and activated sample of **Pr-LOF**.



**Figure S3.** FTIR spectra of the as-synthesized and activated LOFs samples.

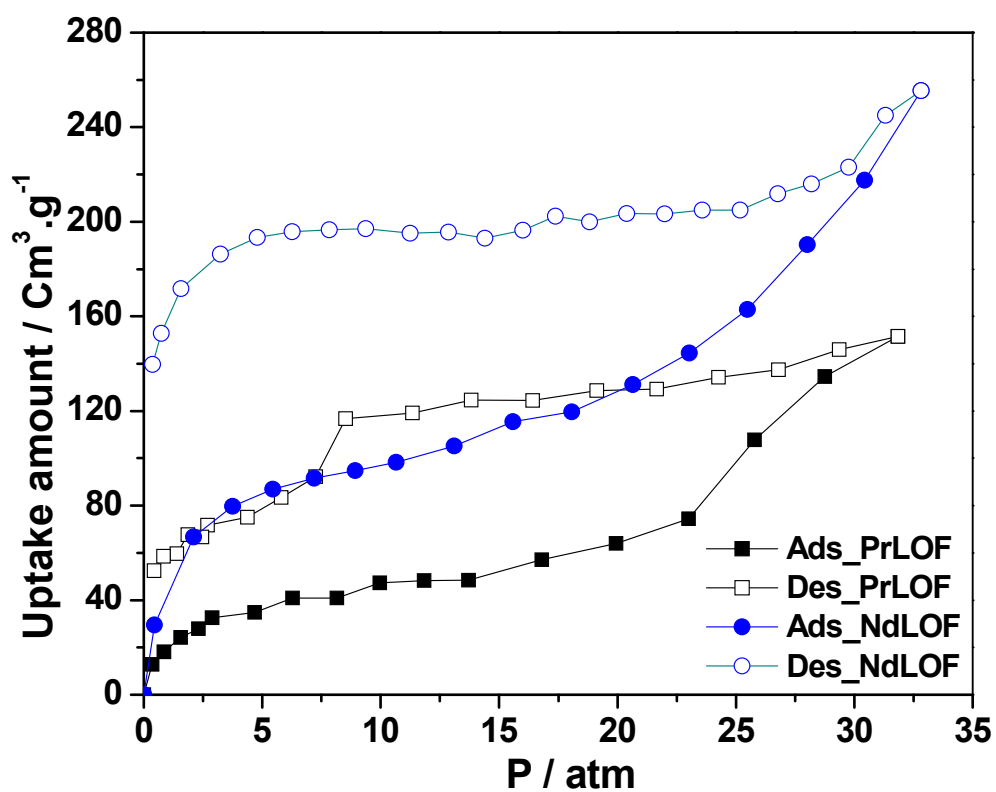


**Figure S4.** Relationship between ion radius and surface area.



**Figure S5.** Pore size distribution of **Pr-LOF** and **Y-LOF** calculated by DFT method.  
Calc. Model: N<sub>2</sub> at 77 K on carbon (slit/cylinder pore, NLDFT equilibrium model).





**Figure S6.** High pressure CO<sub>2</sub> adsorption (filled shapes) and desorption (open shapes) isotherms for PrLOF and NdLOF at 273 K.

The selectivity of CO<sub>2</sub>/N<sub>2</sub>, CH<sub>4</sub>/N<sub>2</sub> and CO<sub>2</sub>/CH<sub>4</sub> for **Pr-LOF** were calculated from the Henry constants. The experimental adsorption isotherms were analyzed by using single Langmuir isotherms [Eq (1)].

$$V = \frac{V_1 K_1 P}{1 + K_1 P} \quad (1)$$

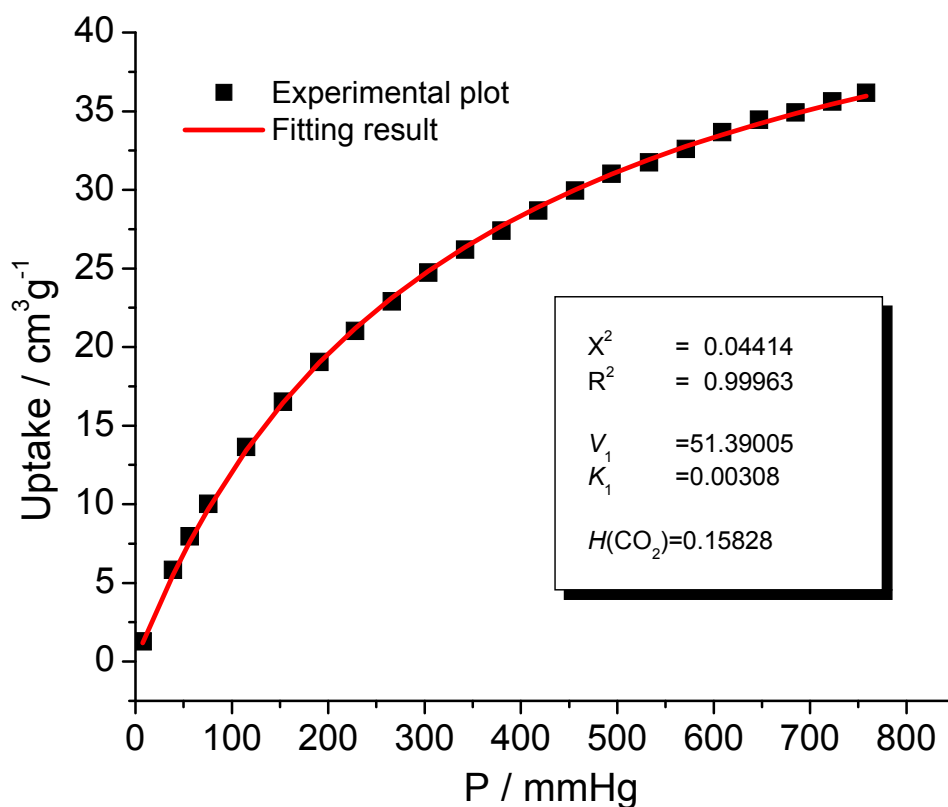
$V$ , the total volume adsorbed of gas;  $P$ , the applied pressure;  $V_1$ , calculated adsorbed volume of CH<sub>4</sub>;  $K_1$ , calculated affinity constants;

Fitting of the adsorption branch for CO<sub>2</sub>, CH<sub>4</sub> and N<sub>2</sub> based on the Langmuir isotherm model allowed us to calculate the Henry constants,  $H=K_1 \times V_1$ .

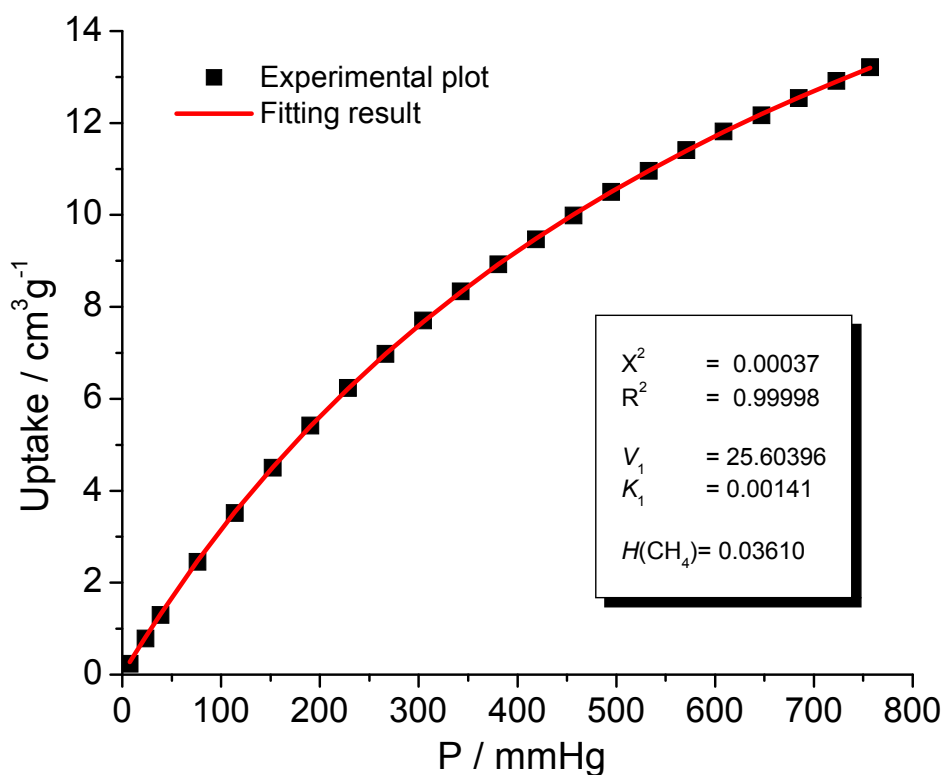
The Henry law selectivity for gas  $i$  over gas  $j$  is then expressed by Equation:

$$S_{i/j} = \frac{H_i}{H_j} \quad (2)$$

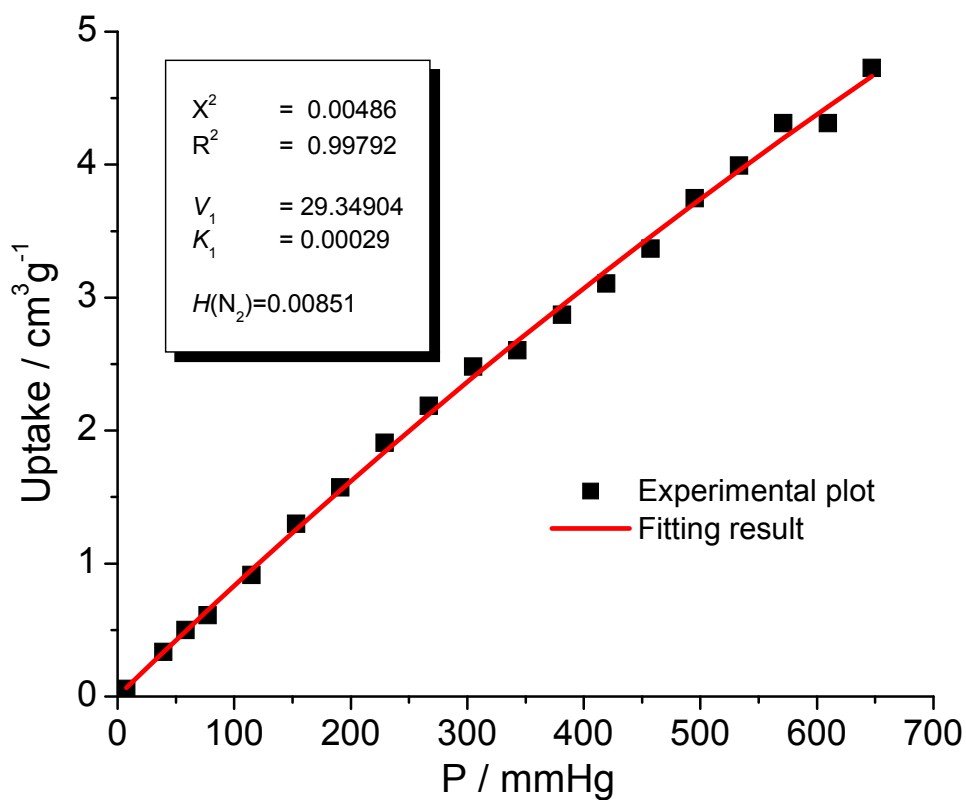
The fitting results are showed in Figure S7-S9.



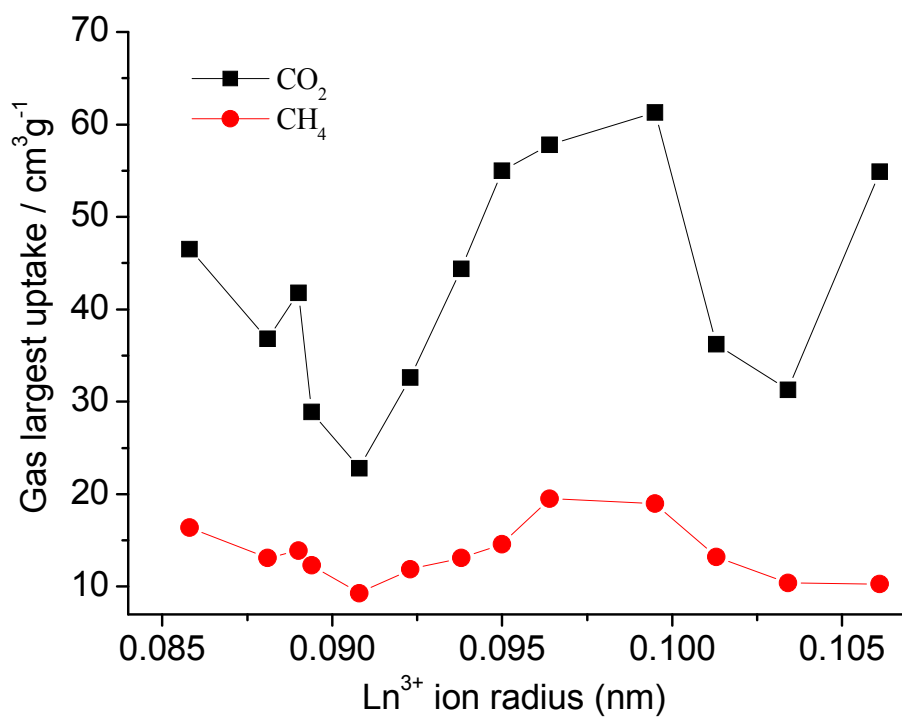
**Figure S7.** CO<sub>2</sub> isotherm adsorption branch of **Pr-LOF** (filled shape) and fitting based on single Langmuir isotherm model (red line).  $V_1$ , calculated adsorbed volume of CO<sub>2</sub>;  $K_1$ , calculated affinity constants;  $X^2$  and  $R^2$ , fitting error;  $H$ , Herry's law constant,  $H(\text{CO}_2)=K_1 \times V_1$  (cm<sup>3</sup>·g<sup>-1</sup>·mmHg<sup>-1</sup>).



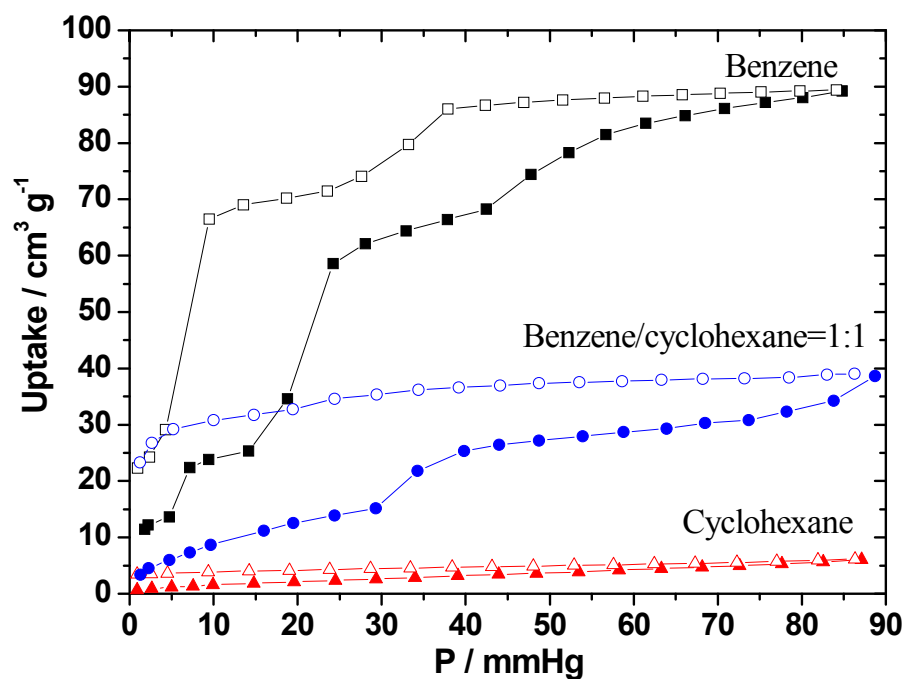
**Figure S8.** CH<sub>4</sub> isotherm adsorption branch of **Pr-LOF** (filled shape) and fitting based on single Langmuir isotherm model (red line).  $V_1$ , calculated adsorbed volume of CH<sub>4</sub>;  $K_1$ , calculated affinity constants;  $X^2$  and  $R^2$ , fitting error;  $H$ , Herry's law constant,  $H(\text{CH}_4)=K_1 \times V_1$  (cm<sup>3</sup>·g<sup>-1</sup>·mmHg<sup>-1</sup>).



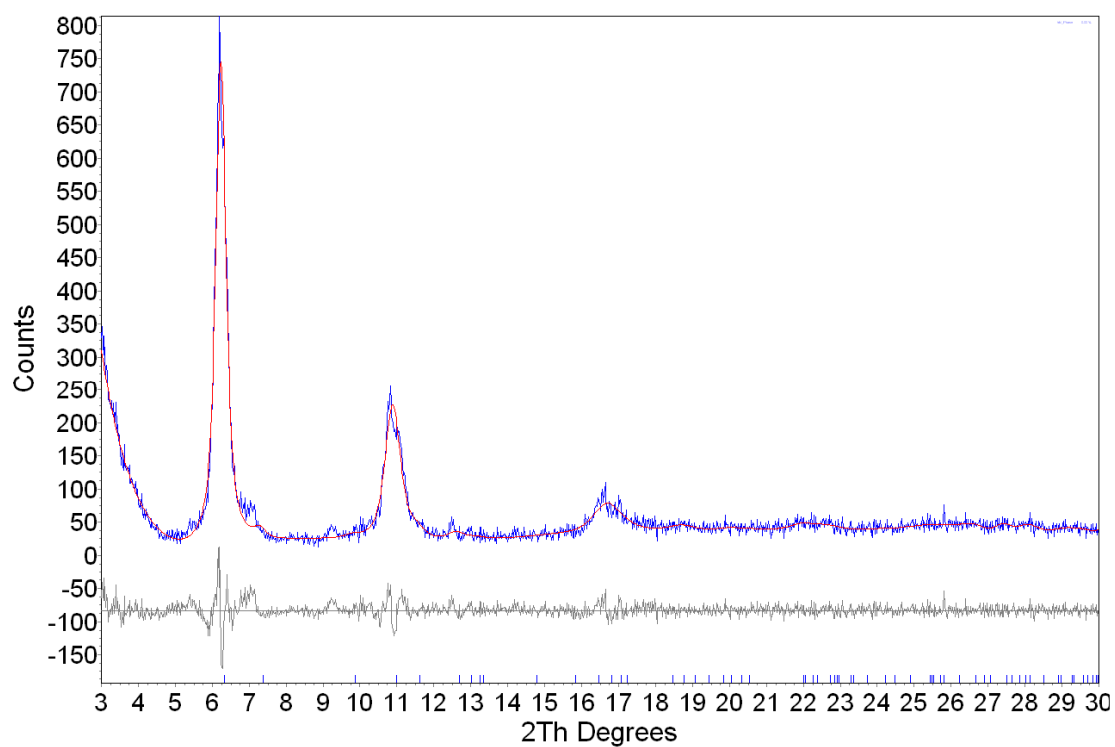
**Figure S9.** N<sub>2</sub> isotherm adsorption branch of Pr-LOF (filled shape) and fitting based on single Langmuir isotherm model (red line).  $V_1$ , calculated adsorbed volume of N<sub>2</sub>;  $K_1$ , calculated affinity constants;  $X^2$  and  $R^2$ , fitting error;  $H$ , Herry's law constant,  $H(N_2)=K_1 \times V_1$  (cm<sup>3</sup>·g<sup>-1</sup>·mmHg<sup>-1</sup>).



**Figure S10.** Relationship between lanthanide ion radius, and gas uptakes.



**Figure S11.** Ce-LOF gave the highest selectivity of benzene/cyclohexane adsorption at 298 K. The blue cycle plots show the sorption of benzene/cyclohexane mixture with volume ratio 1:1.



**Figure 12S.** Powder XRD patterns of Nd-LOF indexed by program TOPAS with a hexagonal  $P6_122$  space group ( $a = 16.17(6) \text{ \AA}$ ,  $c = 25.57(13) \text{ \AA}$ ).



**Table S3.** Summary of gas adsorption test results.

Materials	Ln <sup>3+</sup> ion radius (pm)	S <sub>BET</sub> (m <sup>2</sup> /g)	Pore volume (cm <sup>3</sup> /g)	CO <sub>2</sub> uptake (cm <sup>3</sup> /g)	CH <sub>4</sub> uptake (cm <sup>3</sup> /g)
<b>Y-LOF</b>	89	667	0.44	41.8	13.9
<b>La-LOF</b>	106.1	351	0.31	54.9	10.3
<b>Ce-LOF</b>	103.4	363	0.32	31.3	10.4
<b>Pr-LOF</b>	101.3	484	0.30	36.2	13.2
<b>Nd-LOF</b>	99.5	477	0.29	61.3	19.0
<b>Sm-LOF</b>	96.4	581	0.35	57.8	19.5
<b>Eu-LOF</b>	95.0	426	0.30	55.0	14.6
<b>Gd-LOF</b>	93.8	535	0.31	44.4	13.1
<b>Tb-LOF</b>	92.3	158	0.13	32.6	11.9
<b>Dy-LOF</b>	90.8	281	0.17	22.8	9.3
<b>Ho-LOF</b>	89.4	233	0.14	28.9	12.3
<b>Er-LOF</b>	88.1	283	0.20	36.8	13.1
<b>Yb-LOF</b>	85.8	443	0.38	46.5	16.4

**Table S4.** CO<sub>2</sub> uptake at 273K and 1 atm of lanthanide-based MOFs.

Materials	Uptake [cm <sup>3</sup> /g]	Ref.
Dy(BTC)(H <sub>2</sub> O)·DMF	189	[1]
[Y <sub>2</sub> (TPO) <sub>2</sub> (HCOO)]·(Me <sub>2</sub> NH <sub>2</sub> )·(DMF) <sub>4</sub> ·(H <sub>2</sub> O) <sub>6</sub>	66.9	[2]
[Eu(L) <sub>4</sub> ] <sup>5-</sup>	19.5(P/P <sub>0</sub> =0.03)	[3]
{La(cpia)(2H <sub>2</sub> O) <sub>3</sub> ·4H <sub>2</sub> O} <sub>n</sub>	23 (P/P <sub>0</sub> =0.03)	[4]
{KHo(C <sub>2</sub> O <sub>4</sub> ) <sub>2</sub> (H <sub>2</sub> O) <sub>4</sub> } <sub>n</sub>	21.2 (298 K)	[5]
(Yb <sub>4</sub> (μ <sub>4</sub> -H <sub>2</sub> O)(C <sub>24</sub> H <sub>12</sub> N <sub>3</sub> O <sub>6</sub> ) <sub>8/3</sub> (SO <sub>4</sub> ) <sub>2</sub> ·3H <sub>2</sub> O·10DMSO)	220 (195 K)	[6]
Gd(TPO)	285.8 (195 K)	[7]
Er <sub>2</sub> (TBDC) <sub>3</sub> (phen) <sub>2</sub> 34DMF <sub>3</sub> 2H <sub>2</sub> O	51 (195 K)	[8]
Nd(BTB)	61.3	This work

**Table S5.** Benzene and cyclohexane saturate uptake at 298K.

Materials	Benzene uptake (mg/g)	Cyclohexane uptake (mg/g)	Selectivity <sup>a</sup>
<b>La-LOF</b>	189.7	106.7	1.8
<b>Ce-LOF</b>	311.0	22.9	13.6
<b>Pr-LOF</b>	288.2	33.4	8.6
<b>Nd-LOF</b>	174.7	74.6	2.3
<b>Sm-LOF</b>	214.2	155.4	1.4
<b>Tb-LOF</b>	88.5	41.6	2.1
<b>Dy-LOF</b>	116.0	113.5	1.0
<b>{[Zn(<math>\mu_4</math>-TCNQ-TCNQ)bpy]<math>\cdot</math>1.5benzene}<sub>n</sub></b> <sup>b</sup>	80	20	4
<b>MAF-2</b> <sup>c</sup>	206	9	22.9

<sup>a</sup> Selectivity= Benzene uptake/ Cyclohexane uptake.

<sup>b</sup> Ref. 9.

<sup>c</sup> Ref. 10.

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