

Supporting Information

Lattice dynamics in atomically thin sheets of WS₂ and WSe₂

Weijie Zhao^{a,c,#}, Zohreh Ghorannevis^{a,c,#}, Amara Kiran Kumar^b, Jing Ren Pang^b, Minglin Toh^d, Xin Zhang^e, Christian Kloc^d, Ping Heng Tan^e, Goki Eda^{a,b,c,}*

^a Department of Physics, National University of Singapore, 2 Science Drive 3, Singapore 117542

^b Department of Chemistry, National University of Singapore, 3 Science Drive 3, Singapore 117543

^c Graphene Research Centre, National University of Singapore, 6 Science Drive 2, Singapore 117546

^d School of Materials Science and Engineering, Nanyang Technological University, N4.1 Nanyang Avenue, Singapore 639798

^e State Key Laboratory of Superlattices and Microstructures, Institute of Semiconductors, Chinese Academy of Sciences, Beijing 100083, China

* E-mail: g.eda@nus.edu.sg

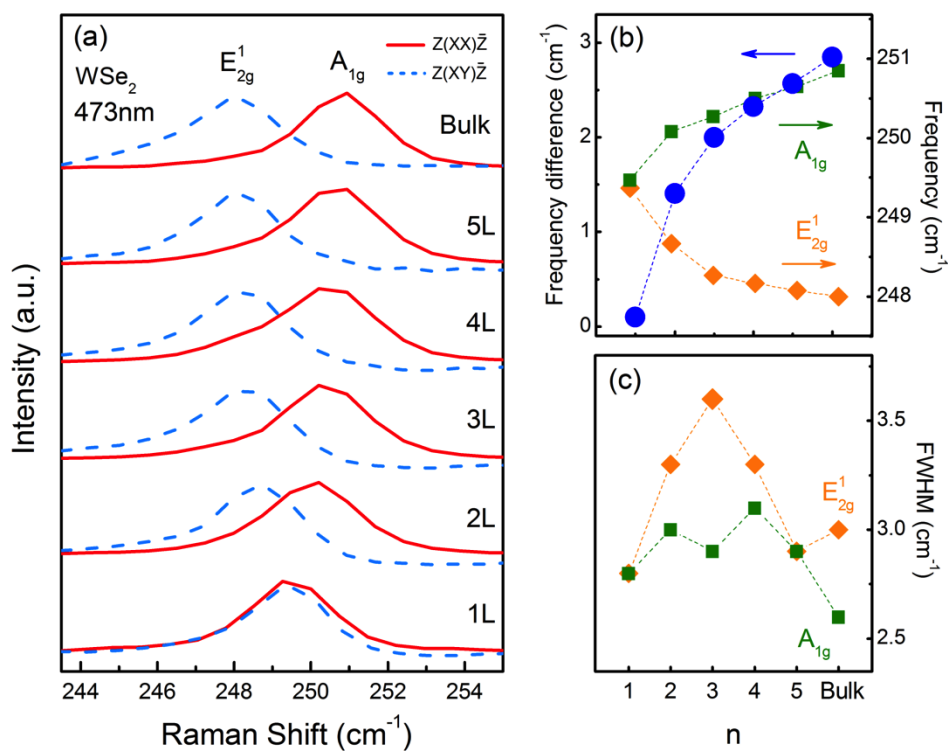


Figure S1 - (a) Raman spectra of 1 to 5L and bulk WSe₂ obtained in the parallel ($Z(XX)\bar{Z}$) and cross ($Z(XY)\bar{Z}$) polarization conditions obtained with 473 nm excitation. The spectra are normalized and vertically offset for clarity. (b) Position of the A_{1g} and E_{2g}^1 modes (right vertical axis) and their difference (left vertical axis) as a function of the number of layers (n). (c) FWHM (right vertical axis) of A_{1g} and E_{2g}^1 modes as a function of the number of layers.

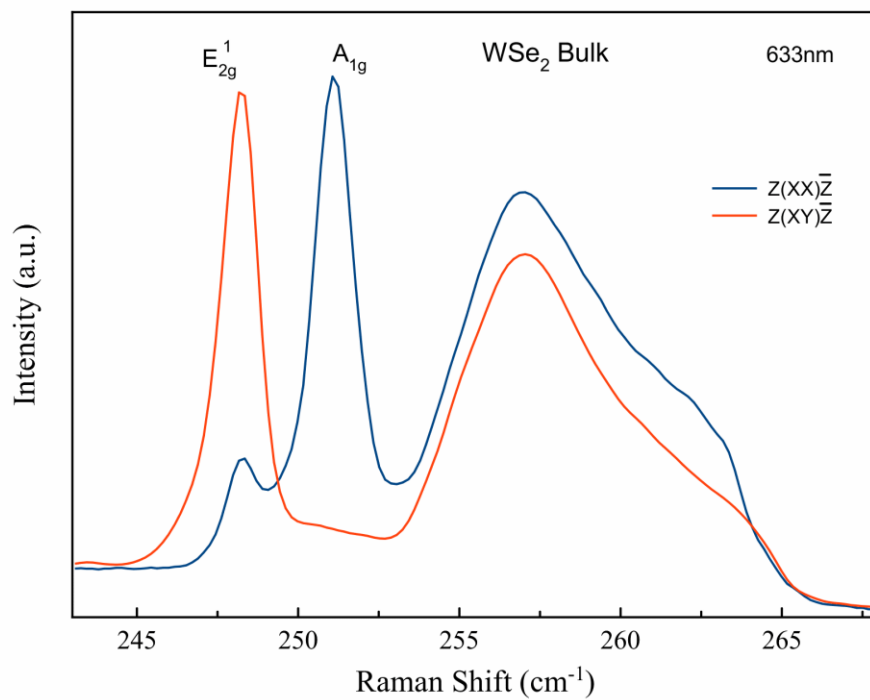


Figure S2 - Raman spectra of bulk WSe₂ obtained in the parallel ($Z(XX)\bar{Z}$) and cross ($Z(XY)\bar{Z}$) polarization conditions with 633 nm excitation. The spectra are normalized.

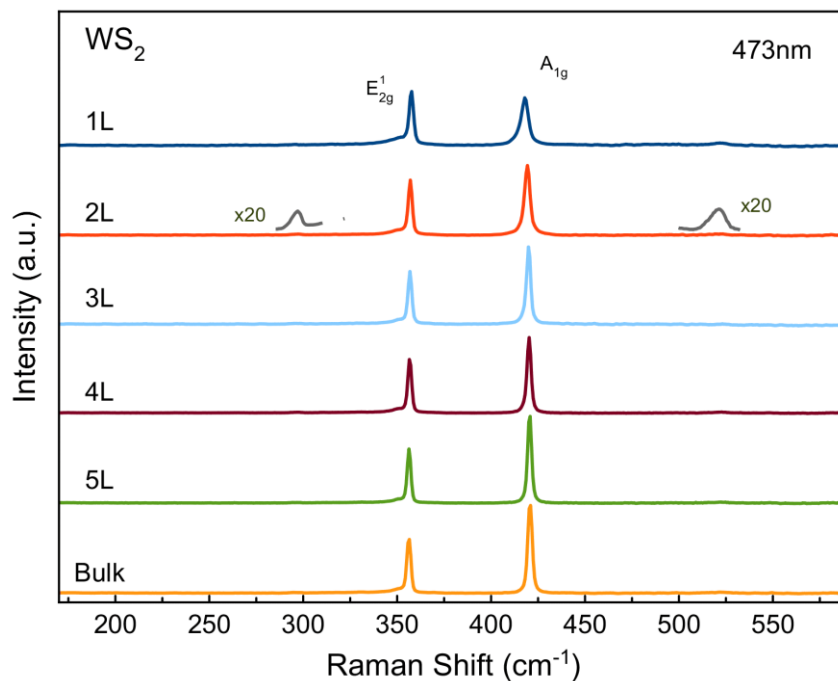


Figure S3 - Raman spectra of 1-5L and bulk WS₂ obtained by 473nm laser excitation.

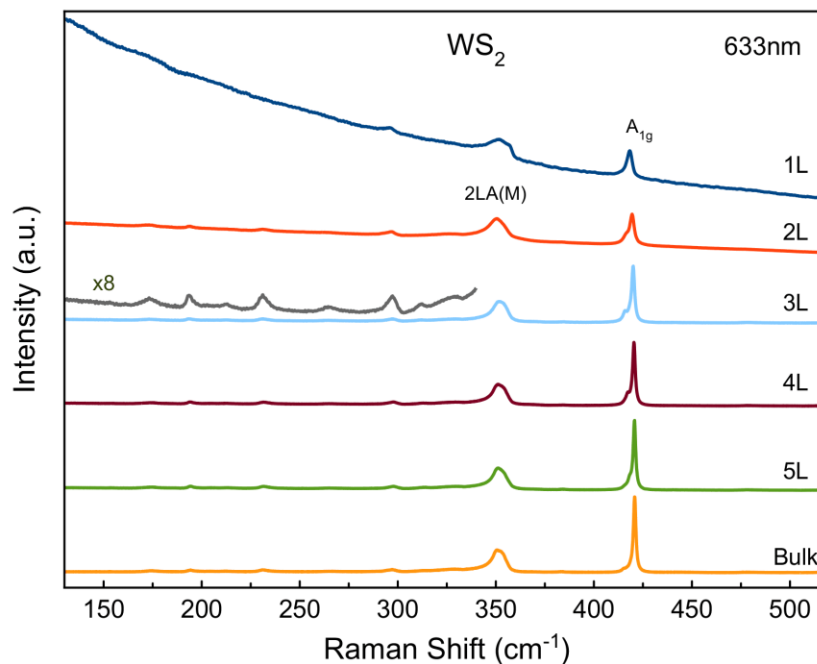


Figure S4 – Unpolarized Raman spectra of 1 to 5L and bulk WS₂ obtained with 633 nm laser excitation. Resonance features are observed in all spectra. Photoluminescence background is observed in monolayer WS₂ spectrum.

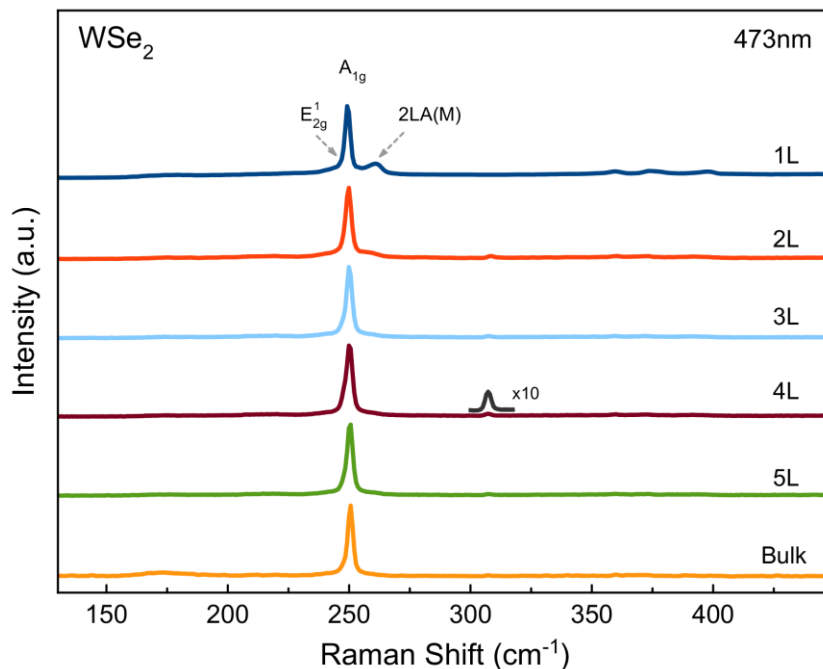


Figure S5 – Unpolarized Raman spectra of 1 to 5L and bulk WSe_2 obtained with 473 nm laser excitation. Some resonance Raman features are observed.

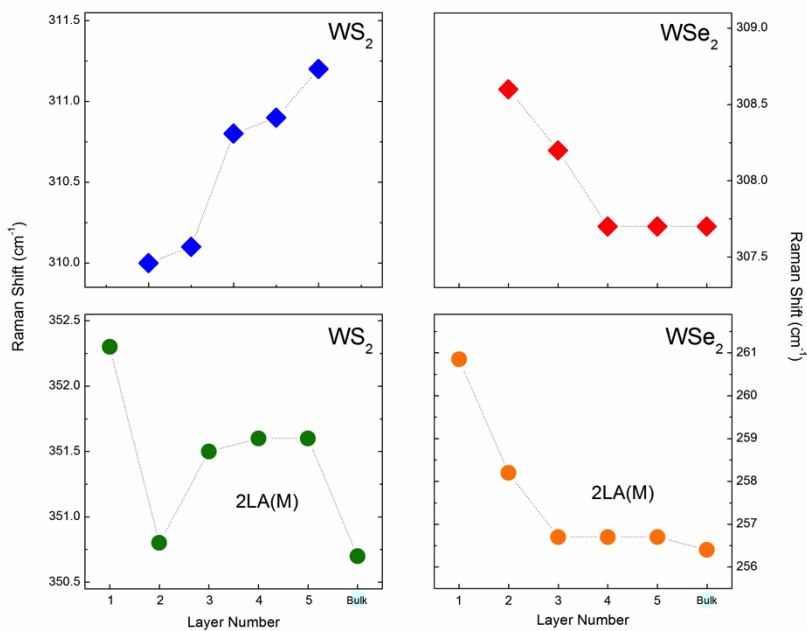


Figure S6 – Thickness dependence of some resonance Raman features observed with 532 nm laser excitation.

Table S1 - Tentative assignments of multiphonon bands observed in the resonance Raman spectra of WS₂ and WSe₂. “y” indicates that the mode is observed. “1L(no)” indicates that the mode is absent in monolayers but observed in multilayers.

Peak(cm ⁻¹)	473nm	532nm	633nm	Possible assignments
WS ₂				
170		1L(no)		$E_{2g}^1(M) - LA(M)$
173		y	y	$E_{2g}^1(M) - LA(M)$
194		y	y	$B_{2g}(M) - LA(M)$
231		y	y	$A_{1g}(M) - LA(M)$
265		y	y	$A_{1g}(M) - ZA(M) ?$
298	y	y	y	$2ZA(M) ?$
311		1L(no)	y	?
326		y	y	$LA(M) + TA(M) ?$
350	y	y	y	$2LA(M)$
522	y	y	y	$E_{2g}^1(M) + LA(M)$
WSe ₂				
136		y	y	$A_{1g}(M) - LA(M)$
260	y	y	y	$2LA(M)$
308	1L(no)	1L(no)		?
360	y	y	y	$2E_{1g}(\Gamma) \text{ or } A_{1g}(M) + TA(M)$
373	y	y	y	$E_{2g}^1(M) + LA(M)$
394	y	y	y	$3LA(M) ?$

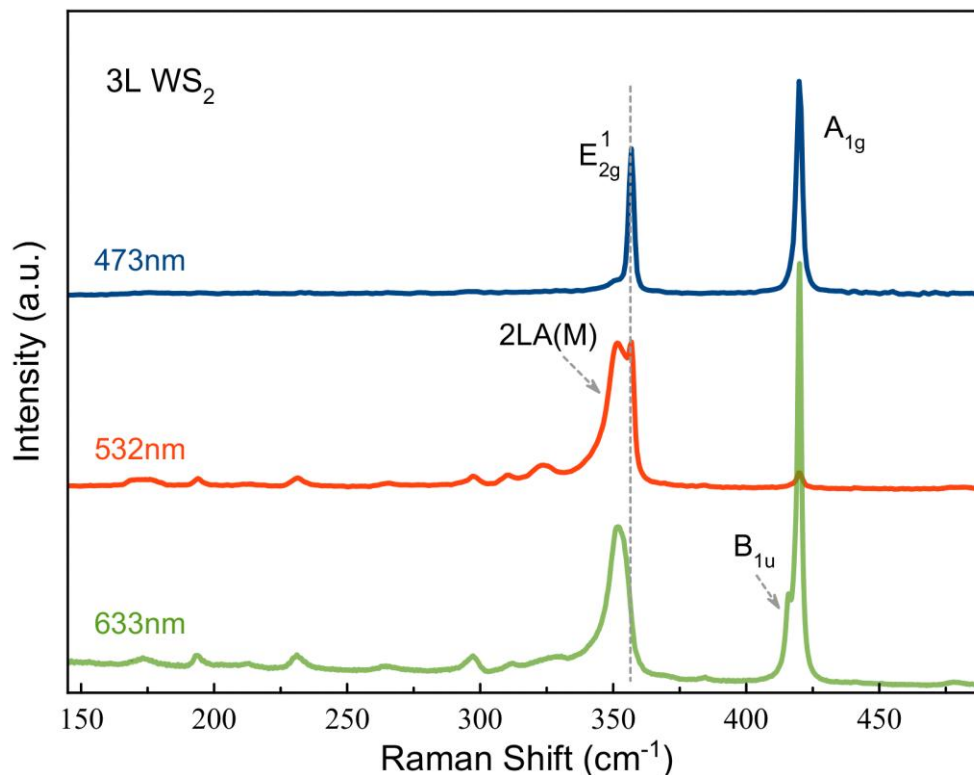


Figure S7 – Unpolarized Raman spectra of 3L WS₂ sample with 473, 532 and 633 nm laser excitations. The spectra are normalized by the E_{2g}^1 peak for 473 and 532nm excitations and by the 2LA(M) mode for 633nm laser excitation. The vertical dashed line indicates the position of E_{2g}^1 peak.

Figure S7 shows the unpolarized Raman spectra of a 3L WS₂ sample obtained using three excitation lasers (473, 532 and 633 nm). For 473 nm excitation, which matches in energy with the density of states absorption peak, 2LA(M) peak is observed as a small left shoulder of the E_{2g}^1 peak. In contrast, the 2LA(M) peak is significantly enhanced with respect to the E_{2g}^1 peak for 532 nm and 633 nm excitations, which are in resonance with the excitonic absorption peaks.

The E_{2g}^1 and A_{1g} modes are both equally enhanced in the interband resonance for 473 nm laser excitation. In contrast, the A_{1g} peak is found to be significantly weak in intensity compared to the E_{2g}^1 peak for 532 nm excitation. For the 633 nm laser

excitation, a reverse effect is observed where the A_{1g} peak is significantly more intense compared to the E_{2g}^1 peak, which is buried in the 2LA(M) peak. This suggests that each Raman mode has different cross-section enhancement for a given excitation condition. The A and B excitonic absorption in WS_2 mainly correspond to the transitions from the d_{xy} and $d_{x^2-y^2}$ states to d_{z^2} states of the tungsten atom [S1, S2, S3]. Thus, electrons excited by the 633 nm laser have a character of the tungsten d_{z^2} orbitals aligned along the c axis perpendicular to the WS_2 basal plane. Since the A_{1g} phonons involve atomic displacements along the c-axis [S4, S5], the A_{1g} phonons can couple more strongly with the excited d_{z^2} states than with the E_{2g}^1 phonons. Consequently, the enhancement of the A_{1g} mode is much stronger than the E_{2g}^1 mode at excitonic resonance for 633 nm laser. A similar effect has been observed in MoS_2 monolayers and nanoparticles [S6, S7]. On the other hand, the reverse effect observed for the 532 nm excitation cannot be explained by the same mechanism. This is likely due to electron-phonon coupling involving not only the d_{z^2} electrons but also other electrons from inter-band transitions [S1, S2, S3].

A peak at $\sim 416\text{ cm}^{-1}$ observed with 633 nm excitation was previously assumed to be a combination of LA and TA phonons at the K point [S8]. However, recent theoretical studies of WS_2 phonon dispersion curves [S9, S10] suggest that this is B_{1u} mode at the Γ point. The B_{1u} mode is the Davydov doublet with the A_{1g} mode [S4, S5, S11]. Studies have shown that this mode is enhanced with increase in disorder in WS_2 nanotubes [S12]. This indicates that the B_{1u} mode may be used for monitoring defects in WS_2 , sheets, similar to the D mode in graphene-based materials [S13], and deserves further investigation.

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