Supporting Information for

## Two Dimensional Dirac Carbon Allotropes from Graphene

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Fig. S1 Phonon band structure of *S*-graphene



**Fig. S2** Snapshots of (a, b)*S*-graphene, (c, d)*D*-graphene and (e, f)*E*-graphene after a 3ps FPMD simulation at 500K



**Fig. S3** Relative energies of new structures. The configuration of uududu allotrope is  $\uparrow\uparrow\downarrow\uparrow\downarrow\uparrow\downarrow\uparrow$ .



Fig. S4 (a) Crystal structure and (b) electronic structure of *A*-graphene



Fig. S5 (a) Crystal structure and (b) electronic structure of *B*-graphene



Fig. S6 (a) Crystal structure and (b) electronic structure of  $T_4$ -graphene



**Fig. S7** crystal structures and band structures of metallic (a, b)  $S_3$ -graphene, (c, d)  $T_3$ -graphene and (e, f) graphene allotrope with configuration of  $\uparrow \uparrow \downarrow \uparrow \downarrow \uparrow$ .