# SUPPORTING INFORMATION

## 1.1 Plot of Gupta Potential and Cutoff



Figure 1.1: Plot of the Gupta Potential function, with different parameters and cutoff in each graph for (a) Pd and (b) Au. Black lines represent the parameters of Cleri and Rosato [1], red lines represent the parameters of Baletto et al. [2], and the blue lines show the polynomial cutoff, with  $C_s$  and  $C_e$  shown by pink and purple dashed lines, respectively.

### 1.2 Long Range Cut-off in the Gupta Potential

The parameters used in reference [2] incorporate a long distance cut-off into the potential for atoms further than 2 neighbours distance away (>  $\sqrt{2}r$ ) [3]. The interatomic potential decays with increasing distance and introducing a cut-off speeds up the energy calculations for large clusters.

A 5<sup>th</sup> order polynomial was introduced, matching that of Baletto *et al.* [2]. For this, a polynomial replacement for the potential that matches the potential function at the cutoff start ( $C_s$ ), and is zero at the cut-off end ( $C_e$ ) is derived. The replacement is applied separately to each exponential component of the Gupta potential. Considering the term:

$$V_{ij}^{r}(r_{ij}) = Ae^{-p(\frac{r_{ij}}{r_0} - 1)}$$
(1.1)

for  $C_s \leq r_{ij} \leq C_e$  we replace the above expression by the following polynomial  $p_1(r_{ij})$ :

$$V_{ij}^{r}(r_{ij}) = p_1(r_{ij}) = a_5(r_{ij} - C_e)^5 + a_4(r_{ij} - C_e)^4 + a_3(r_{ij} - C_e)^3$$
(1.2)

where the coefficients  $a_5$ ,  $a_4$ ,  $a_3$  are chosen to match the function and its first and second derivatives for  $r_{ij} = C_s$ . For  $r = C_e$ ,  $p_1(r_{ij}) = 0$ . The form of the polynomial ensures that the conditions on the function and its first derivative are automatically matched for  $r_{ij} = C_e$ . In the same way, for the term:

$$\left[V_{ij}^{m}(r_{ij})\right]^{\frac{1}{2}} = \zeta e^{-q(\frac{r_{ij}}{r_0} - 1)}$$
(1.3)

the following polynomial,  $p_2(r_{ij})$ , is used:

$$\left[V_{ij}^{m}(r_{ij})\right]^{\frac{1}{2}} = p_{2}(r_{ij}) = x_{5}(r_{ij} - C_{e})^{5} + x_{4}(r_{ij} - C_{e})^{4} + x_{3}(r_{ij} - C_{e})^{3}$$
(1.4)

where the coefficients  $x_5$ ,  $x_4$ ,  $x_3$  are calculated to match the form of the Gupta function. The cut-off parameters used are given in Table 1.1, and included in the potential functions plotted in Appendix 1.1.

	Parameter Set II	
	Pd	Au
$C_s$ (Å)	3.890	4.070
$C_e$ (Å)	4.764	4.984
$a_3$	$-5.732 \ge 10^{-3}$	$-8.105 \ge 10^{-3}$
$a_4$	$-8.477 \ge 10^{-3}$	$-1.110 \ge 10^{-2}$
$a_5$	$-5.723 \ge 10^{-3}$	-6.828 x $10^{-3}$
$x_3$	-3.131	-2.232
$x_4$	-4.861	-3.258
$x_5$	-2.157	-1.383

Table 1.1: Cut-offs and polynomial coefficients used for Au and Pd (to 4 significant figures) for parameter set II

#### **1.3** Energetic Analysis

#### **1.3.1** $Pd_N$ Clusters

12-Vertex Structures: Icosahedra, Ino-Decahedra and Cuboctahedra.



Figure 1.2: Left: Plot of  $E_b$  for  $Pd_N$  structures against N. Solid lines represent the parameter set I of Cleri and Rosato [1], and dashed lines represent the parameter set II of Baletto *et al.* [2]. Right: Plot of  $E_b$  for  $Pd_N$  structures against  $N^{-\frac{1}{3}}$ . In (black squares), I-Dh (red circles) and CO (blue triangles) are shown in both plots;  $E_{coh}$  of 3.89 eV [4]) is displayed as a grey solid line.

Figure 1.2 plots  $E_b$  for Ih, I-Dh and CO structures, with increasing shell sizes k, against N. For N < 100,  $E_b$  rapidly increases, before levelling off as N > 500; this trend is consistent for both parameter sets. Identification between the different structural motifs is energetically difficult, implying that they are all closely competitive in energy at this size. A spacing between trend lines is visible for the two parameter sets: parameter set Irises to a higher level than parameter set II, before flattening out asymptotically relative to  $E_{coh}$ . The difference in gradients between parameter sets I and II can be identified in the right of Figure 1.2 where an approximation to the  $E_{coh}$  is achieved for  $N^{-\frac{1}{3}} \to 0$ when  $N^{-\frac{1}{3}}$  is plotted against  $E_b$ . Linear extrapolation to 0 for parameter set I gives a slightly over-exaggerated  $E_{coh}$  (3.92 eV) compared to the experimentally measured value (3.89 eV [4]), whilst parameter set II offers better agreement to this measurement (3.88 eV).

#### 1.3.2 $Au_N$ Clusters

12-Vertex Structures: Icosahedra, Ino-Decahedra and Cuboctahedra.



Figure 1.3: Main: Plot of  $E_b$  for  $Au_N$  structures against N. Solid lines represent the parameter set I of Cleri and Rosato [1], and dashed lines represent the parameter set II of Baletto *et al.* [2]. Inset: Plot of  $E_b$  for  $Au_N$  structures against  $N^{-\frac{1}{3}}$ . In (black squares), I-Dh (red circles) and CO (blue triangles) are shown in both plots; the bulk  $E_{coh}$  (3.81 eV [4]) is displayed as a grey solid line.

Figure 1.3 compares  $E_b$  for the high-symmetry Au<sub>N</sub> structures of the Ih, I-Dh and CO geometries. Similar trends to the results of Pd<sub>N</sub> are seen with sharply increasing  $E_b$ for N < 100, levelling out asymptotically towards the bulk  $E_{coh}$  value of 3.81 eV [4] as  $N \to \infty$ . Parameter set II tends to a higher value of  $E_b$  than parameter set I, an inverse of the results for  $\mathrm{Pd}_N$  clusters (Figure 1.2). Attention to the inset, which relates  $E_b$  to the bulk limit  $(N^{-\frac{1}{3}} \to 0)$ , suggests that the parameter set I underestimates the extrapolated bulk  $E_{coh}$  value (3.77 eV), whilst parameter set II does not (3.81 eV).

Structural preferences are difficult to identify in Figure 1.3; we can calculate relative stabilities ( $\Delta E_b$ ) of different geometries with identical nuclearities using:

$$\Delta E_b = E_{b_{Ih}} - E_{b_x} \tag{1.5}$$

where the binding energies of I-Dh or CO can be directly compared with Ih  $(E_{b_{Ih}})$  when substituted in for  $E_{b_x}$ . Positive values indicate reduced stability, and a negative value indicates increased stability, relative to the Ih; thus  $\Delta E_b$  is plotted in Figure 1.4 for  $Au_N$ clusters.

For parameter set I we see intersection of  $E_{b_{Ih}}$  at N = 682 by  $\Delta E_{b_{I-Dh}}$  and at N = 923by  $\Delta E_{b_{CO}}$ , calculated using a linear fit. For parameter set II these intersections of  $E_{b_{Ih}}$ are at lower N: 284 and 393 for  $\Delta E_{b_{I-Dh}}$  and  $\Delta E_{b_{CO}}$ , respectively. The values of N for these intersections are much less than found for  $Pd_N$ , implying relative instability of the close-packed cluster geometries (Ih, I-Dh) with respect to the crystalline bulk fragments for Au nanoparticles.



Figure 1.4: Plot of  $\Delta E_b$  for Ih (black), I-Dh (red) and CO (blue) Au<sub>N</sub> structures against N. Solid lines represent parameter set I of Cleri and Rosato [1], and dashed lines represent parameter set II of Baletto *et al.* [2].



1.3.3  $(Pd_{core}Au_{shell})_N$  Clusters

Figure 1.5: Plots of  $\Delta$  against N for the  $Pd_{core}Au_{shell}$  12-vertex high-symmetry structures (solid lines), using parameter set I of Cleri and Rosato [1], with cores: (a)  $Pd_1$  (b)  $Pd_{13}$  (c)  $Pd_{55}$  (d)  $Au_{147}$ . In (black squares), I-Dh (red circles) and CO (blue triangles) are shown, with  $Au_N$  (dashed lines) also plotted.

## LIST OF REFERENCES

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