## **Electronic Supplementary Information**







Figure 3: (d)



Figure 14: (b)



Figure 14: (c)



Figure 14: (d)

## Accuracy of Free-Energy Calculations

Obviously, the accuracy of our calculated free energy per chain  $f_c$  determines the reliability of our constructed phase diagrams. This accuracy depends on several factors, including the cell length and its discretization (number of subintervals) m in each dimension, the chain contour discretization n, and the convergence criterion  $\epsilon$  for iterating SCF equations. The choice of m, n and  $\epsilon$  are dictated by the boundary conditions in the confined dimension and the sharpness of A-B interfaces in each dimension (i.e.,  $\chi N$  and the morphology). When the Dirichlet boundary conditions are used, the accuracy is mainly determined by the spatial discretization in the confined dimension, and the detailed numerical analysis in our previous work<sup>31</sup> justifies our statement that an accuracy of  $< 10^{-3}$  in  $f_c$  is reached in our calculations.

When the Neumann boundary conditions are used, the accuracy is mainly determined by the sharpness of A-B interfaces. We therefore perform 1D calculations of =(1)between two neutral surfaces separated at  $D = L_0$  (our bulk calculations at  $\chi N = 20$  give  $L_0 \approx 4.045 R_g$ , in good agreement with Ref. [27]). The results shown in Fig. 15 clearly justify our statement that an accuracy of  $< 10^{-3}$  in  $f_c$  is reached in our calculations. Note that the A-B interfaces in =(1.5) under the same conditions are smoother, resulting in higher accuracy in  $f_c$  (data not shown).



Figure 15: Accuracy of the obtained free energy per chain  $f_c$  in 1D calculations of =(1) between two neutral surfaces separated at  $D = L_0$  without the hard-surface effect.

## Stability of $T_1$ at $\chi N = 20$

Using the same discretization and convergence criterion as given in Sec. 2, we have performed some calculations of  $L_0$ -thick films between dissimilar surfaces without the hardsurface effect, where we set  $\chi N = 20$  and  $\Lambda_l = 10$ . Fig. 16 compares the obtained free energies of =(1), =(1.5), T\_1(2D) and T\_1(3D); the results are qualitatively the same as those shown in Fig. 10, including all the free-energy components (data not shown). Our results in Sec. 3.2 (including those on the lateral periods of T<sub>1</sub>; data not shown) therefore remain valid at  $\chi N = 20$ . Comparing to Fig. 7 at  $\chi N = 15$ , we find that both the stable regions of T<sub>1</sub>(2D) and T<sub>1</sub>(3D) over parallel lamellae shrink and are shifted to larger  $|\Lambda_u|$ -values with increasing  $\chi N$ , and that T<sub>1</sub>(2D) is no longer stable against T<sub>1</sub>(3D) at  $\chi N = 20$  due to its too large  $f_{AB}$  (data not shown).



Figure 16: Free energy per chain  $f_c$  of various morphologies at  $\chi N = 20$ ,  $D = L_0 \approx 4.045 R_g$  and  $\Lambda_l = 10$  obtained from 3D calculations without the hard-surface effect.