

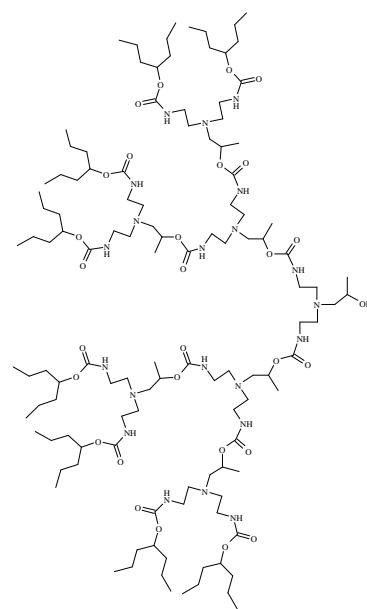
Synthesis and Thermal Studies of Aliphatic Polyurethane Dendrimers: A Geometric Approach to the Flory-Fox equation for Dendrimer Glass Transition Temperature.

Alison Stoddart, W. James Feast and Steve P. Rannard*

Electronic Supporting Information

Synthetic Details

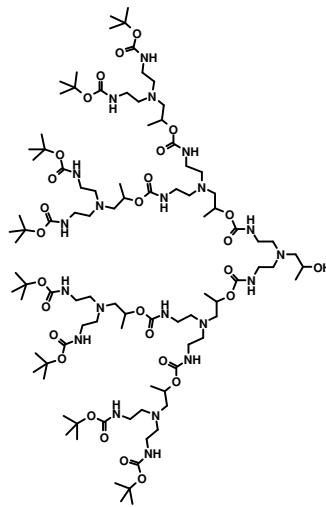
Synthesis of 6a:



CDI (0.75 g, 4.62 mmol) was added to a stirred solution of **5a** (4.3 g, 3.89 mmol) in toluene (50 mL). The mixture was heated at 60°C for 4 hrs. Subsequently, the reaction mixture was analysed by ¹H NMR spectroscopy and interpretation of the spectrum indicated there was no evidence of the starting materials. The branching unit **4** (0.31 g, 1.95 mmol) was added and the solution was heated for 1 day at 60°C. The reaction mixture was concentrated *in vacuo* and redissolved in CH₂Cl₂ (100 mL). The organic phase was subsequently washed with water (3 x 100 mL), dried over MgSO₄ and the solvent removed using a rotary evaporator. The resulting pale yellow oil was purified by column chromatography (silica gel, eluting with EtOAc increasing to EtOAc:MeOH 100:5) and the colourless oil obtained was dried under vacuum (10⁻¹ mbar) to give **6a** as a colourless oil (2.1 g, 44%). T_g = 11°C. Found C, 59.08; H, 9.72; N, 12.02%. C₁₁₉H₂₃₃O₂₉N₂₁ requires, C, 59.01; H, 9.70; N, 12.14%. ¹³C NMR (62.9 MHz, CD₃OD) δ(ppm)= 14.5, 19.0, 19.6, 21.0, 37.9, 40.1, 55.6, 61.0, 64.1, 66.1, 70.7, 75.2, 158.7, 159.2. ¹H NMR (250 MHz, CD₃OD) δ(ppm)= 0.92 (t, J=7Hz, 48H), 1.12 (d, J=6Hz, 3H), 1.20 (d, J=6Hz, 18H), 1.36 (m, 32H), 1.49 (m, 32H), 2.45-2.62 (m, 42H), 3.10-3.27 (m, 28H), 3.78 (m, 1H), 4.73 (m, 8H), 4.81

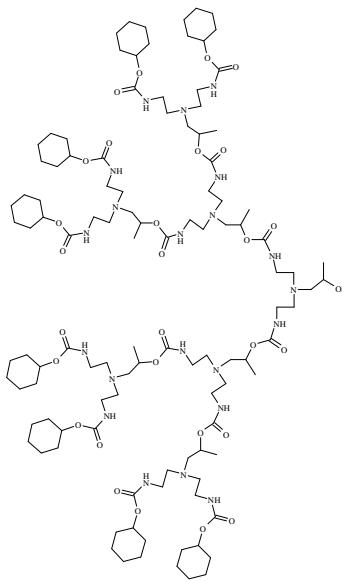
(m, obscured by water peak, 6H), 6.64 (s, br, O(CO)NHCH₂CH₂), 6.71 (s, br, O(CO)NHCH₂CH₂), 6.85 (s, br, O(CO)NHCH₂CH₂). *m/z* (MALDI TOF (Voyager) MS) 2423.6 [M+H]⁺, 2445.2 [M+Na]⁺, 2461.2 [M+K]⁺, calculated M_w = 2422.25. GPC; M_w = 2830, PDI = 1.02.

Synthesis of 6b:



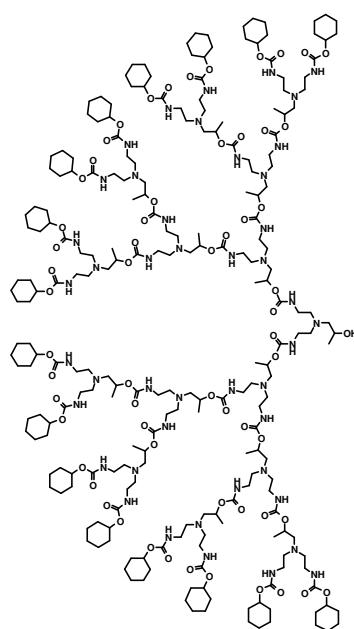
The procedure was similar to that described for the synthesis of, but using **5b** as the starting material. The oil obtained was purified by column chromatography (silica gel, eluting with EtOAc increasing to EtOAc:MeOH, 100:5) and then purified by preparative GPC (Biobeads, eluting with toluene) to give **6b** as a colourless amorphous solid (48%). $T_g = 40^\circ\text{C}$. Found C, 54.16; H, 9.08; N, 13.83%. $C_{95}\text{H}_{185}\text{O}_{29}\text{N}_{21}$ requires, C, 54.71; H, 8.94; N, 14.10%. ^{13}C NMR (62.9 MHz, CD_3OD) δ (ppm)= 19.0, 21.0, 28.9, 39.6, 40.0, 55.6, 55.9, 61.0, 64.0, 66.0, 70.7, 79.9, 158.3, 158.7, 158.8. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 1.12 (d, $J=6\text{Hz}$, 3H), 1.20 (d, $J=6.4\text{Hz}$, 18H), 1.44 (s, 72H), 2.41-2.64 (m, 42H), 3.04-3.24 (m, 28H), 3.78 (m, 1H), 4.85 (m, obscured by water peak, 6H), 6.42 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.71 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.85 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$). m/z (ES MS) 2108.2 [$\text{M}+\text{Na}$] $^+$, 1054.4 [$\text{M}+\text{H}$] $^{2+}$, 1065.4 [$\text{M}+\text{Na}$] $^{2+}$. m/z (MALDI TOF (Voyager) MS) 2086 [$\text{M}+\text{H}$] $^+$, 2108 [$\text{M}+\text{Na}$] $^+$, 2124 [$\text{M}+\text{K}$] $^+$ – and sets of similar peaks at 100 mass intervals below the molecular ion, calculated $M_w = 2085.61$. GPC; $M_w = 2300$, PDI = 1.01.

Synthesis of 6c:



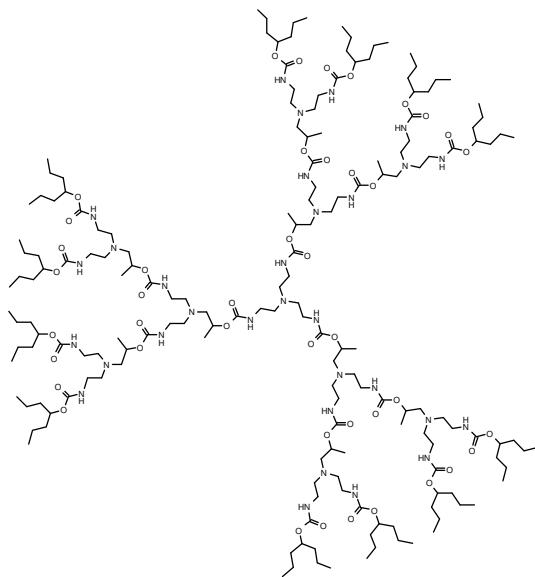
The procedure was similar to that described above, but using **5c** as the starting material. The colourless oil obtained after silica gel chromatography (eluting with EtOAc increasing to EtOAc:MeOH 100:5) was purified further by preparative GPC (Biobeads, eluting with toluene) to give **6c** as a colourless amorphous solid (28%). $T_g = 40^\circ\text{C}$. Found C, 58.05; H, 8.85; N, 12.69%. $C_{111}\text{H}_{201}\text{O}_{29}\text{N}_{21}$ requires, C, 58.12; H, 8.83; N, 12.82%. ^{13}C NMR (100 MHz, CD_3OD) δ (ppm)= 19.0, 21.0, 24.9, 26.6, 33.2, 39.9, 40.1, 40.5, 55.5, 55.7, 55.9, 60.9, 64.1, 66.0, 70.7, 73.9, 157.6, 157.7, 157.8. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 1.12 (d, $J=6.4\text{Hz}$, 3H), 1.45 (d, $J=5.6\text{Hz}$, 18H), 1.25-1.42 (m, 40H), 1.56 (m, 8H), 1.75 (m, 16H), 1.85 (m, 16H), 2.42-2.69 (m, 42H), 3.15-3.25 (m, 28H), 3.78 (m, 1H), 4.57 (m, 8H), 4.84 (m, obscured by water peak, 6H), 6.59 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.71 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.86 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$). m/z (MALDI TOF (Voyager) MS) 2294.0 [$\text{M}+\text{H}$] $^+$, 2316.2 [$\text{M}+\text{Na}$] $^+$, 2331.2 [$\text{M}+\text{K}$] $^+$, calculated $M_w = 2293.91$. GPC; $M_w = 2440$, PDI = 1.01.

Synthesis of 7c:



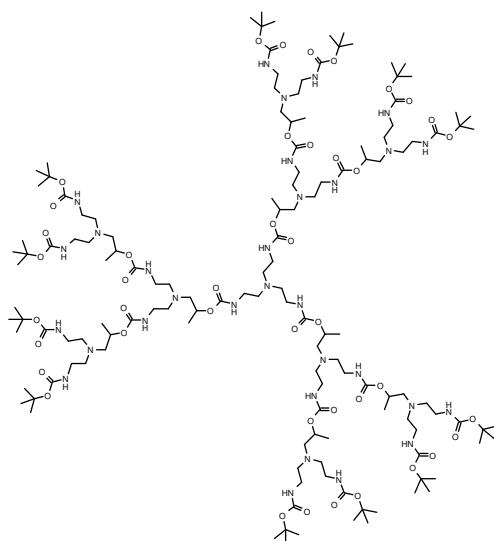
The procedure was similar to that described for the synthesis of **6a**, but using **6c** as the starting material. The crude product obtained was purified by column chromatography (silica gel, eluting with EtOAc:MeOH, 100:5) and the colourless solid obtained was purified by preparative GPC (Biobeads, eluting with toluene) to give *compound CG4OH* as a colourless amorphous solid (14%). $T_g = 48^\circ\text{C}$. Found C, 56.95; H, 8.66; N, 12.57%. $C_{231}H_{410}O_{61}N_{45}$ requires, C, 57.79; H, 8.75; N, 13.13%. ^{13}C NMR (100 MHz, CD_3OD) δ (ppm)= 19.0, 19.1, 21.1, 24.9, 26.6, 33.2, 39.9, 40.1, 40.4, 40.5, 55.5, 55.7, 60.9, 64.1, 66.0, 70.7, 74.0, 158.6, 158.7, 158.8. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 1.12 (d, $J=6\text{Hz}$, 3H), 1.19-1.45 (m, 122H), 1.56 (m, 16H), 1.74 (m, 36H), 1.85 (m, 36H), 2.44-2.68 (m, 88H), 3.11-3.20 (m, 60H), 3.78 (m, 1H), 4.57 (m, 16H), 4.84 (m, 14H), 6.59 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.70 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$), 6.85 (s, br, $\text{O}(\text{CO})\text{NHCH}_2\text{CH}_2$). m/z (MALDI TOF (Voyager) MS) 4801.4 [$\text{M}+\text{H}]^+$, 4823.4 [$\text{M}+\text{Na}]^+$, 4839.3 [$\text{M}+\text{K}]^+$, calculated $M_w = 4801.05$. GPC; $M_w = 4190$, PDI = 1.02.

Synthesis of G2-4-heptyl Dendrimer TAEA:



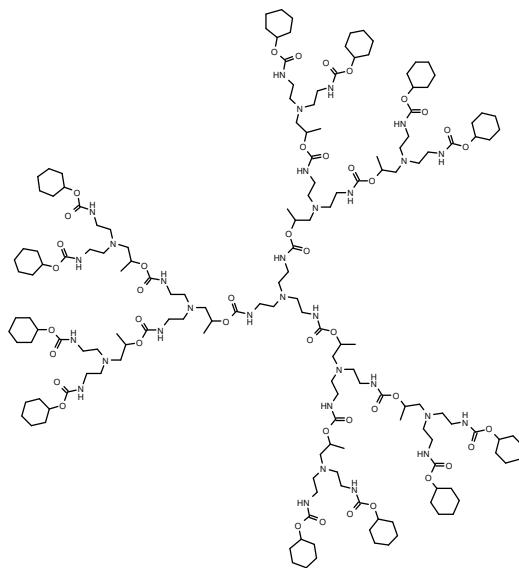
CDI (0.52 g, 3.21 mmol) was added to a stirred solution of **5a** (3.2 g, 2.90 mmol) in toluene (100 mL). The mixture was heated at 60°C for 4 hrs. Subsequently, the reaction mixture was analysed by ^1H NMR spectroscopy and interpretation of the spectrum indicated there was no evidence of the starting materials. Tris(2-aminoethyl)amine (0.14 g, 0.96 mmol) was added and the solution was heated for 20 hrs at 60°C . The reaction mixture was concentrated *in vacuo* and redissolved in CH_2Cl_2 (150 mL). The organic phase was subsequently washed with water (3 x 150 mL), dried over MgSO_4 and the solvent removed using the rotary evaporator. The crude product was purified by column chromatography (silica gel, eluting with EtOAc increasing to EtOAc:MeOH 100:5) and the colourless oil obtained was purified further by preparative GPC (Biobeads, eluting with toluene) to give G2-4-heptyl Dendrimer TAEA as a sticky colourless oil (0.86 g, 24%). $T_g = 17^\circ\text{C}$. Found C, 58.38; H, 9.55; N, 12.15%. $C_{174}H_{339}O_{42}N_{31}$ requires, C, 59.07; H, 9.66; N, 12.27%. ^{13}C NMR (62.9 MHz, CD_3OD) δ (ppm)= 14.5, 19.1, 19.6, 37.9, 40.0, 55.2, 55.6, 60.9, 70.7, 75.1, 158.6, 159.1. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 0.92 (t, $J=7.2\text{Hz}$, 72H), 1.20 (d, $J=6\text{Hz}$, 27H), 1.36 (m, 48H), 1.50 (m, 48H), 2.50-2.62 (m, 60H), 3.16 (m, 42H), 4.73 (m, 12H), 4.86 (m, 9H), 6.65 (s, br, OC(O)NHCH_2), 6.76 (s, br, OC(O)NHCH_2). m/z (ES MS) 3558.5 [$\text{M}+\text{Na}]^+$, 1791.5 [$\text{M}+2\text{Na}]^{2+}$. m/z (MALDI TOF (Kratos) MS) 3558 [$\text{M}+\text{Na}]^+$, calculated $M_w = 3537.74$. GPC; $M_w = 3680$, PDI = 1.01.

Synthesis of G2-*t*-butyl Dendrimer TAEA:



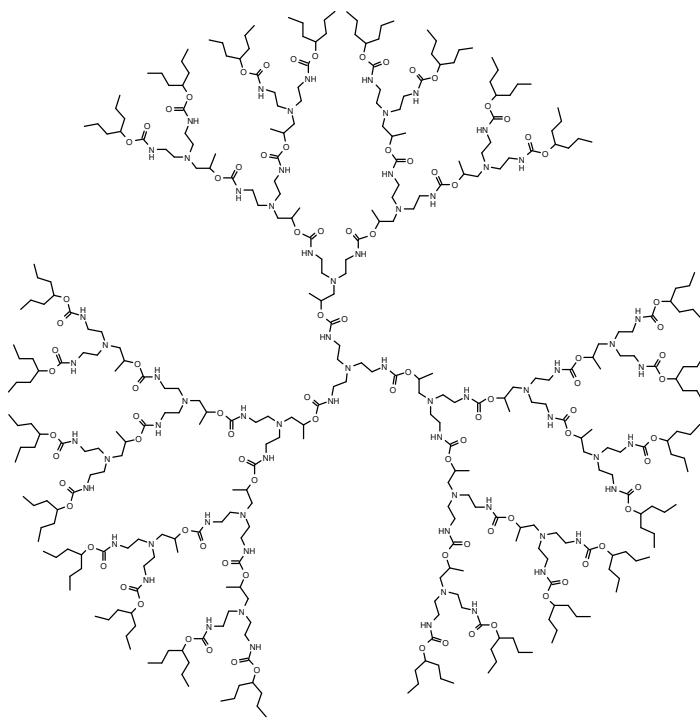
The procedure was the same as that described for the synthesis and purification of G2-4-heptyl Dendrimer TAEA but **5b** was used as the starting material to give G2-cyclohexyl Dendrimer TAEA as colourless oil (32%). $T_g = 47^\circ\text{C}$. Found C, 55.11; H, 8.79; N, 13.46%. $\text{C}_{138}\text{H}_{267}\text{O}_{42}\text{N}_{31}$ requires, C, 54.65; H, 8.87; N, 14.32%. ^{13}C NMR (62.9 MHz, CD_3OD) δ (ppm)= 19.0, 28.9, 39.5, 40.0, 55.2, 55.7, 60.9, 70.6, 80.0, 158.4, 158.7. ^1H NMR (250 MHz, CD_3OD) δ (ppm)= 1.21 (d, $J=6\text{Hz}$, 27H), 1.45 (s, 108H), 2.50-2.75 (m, 60H), 3.05-3.25 (m, 42H), 4.85 (m, obscured by water peak, 9H), 6.46 (s, br, OC(O)NHCH_2), 6.76 (s, br, OC(O)NHCH_2). m/z (ES MS) 3055.1 [$\text{M}+\text{Na}$] $^+$, 1539.0 [$\text{M}/2+\text{Na}$] $^+$. m/z (MALDI TOF (Kratos) MS) 3039 [$\text{M}+\text{H}$] $^+$, calculated $M_w = 3032.78$. GPC; $M_w = 3120$, PDI = 1.02.

Synthesis of G2-cyclohexyl Dendrimer TAEA:



The procedure was similar to that described for the synthesis of G2-4-heptyl Dendrimer TAEA but **5c** was used as the starting material. The purification step was achieved by column chromatography (silica gel, eluting with EtOAc increasing to EtOAc:MeOH 100:5) and the oil obtained was purified further by preparative GPC (Biobeads, eluting with toluene) to give G2-cyclohexyl Dendrimer TAEA as a colourless amorphous solid (41%). $T_g = 44^\circ\text{C}$. Found C, 57.43; H, 8.70; N, 12.75%. $\text{C}_{162}\text{H}_{291}\text{O}_{42}\text{N}_{31}$ requires, C, 58.16; H, 8.77; N, 12.98%. ^{13}C NMR (62.9 MHz, CD_3OD) δ (ppm)= 19.0, 24.8, 26.5, 33.1, 39.9, 55.5, 60.9, 70.7, 73.9, 158.57, 158.62, 158.7. ^1H NMR (250 MHz, CD_3OD) δ (ppm)= 1.19 (d, $J=5.5\text{Hz}$, 27H), 1.39 (m, 60H), 1.55 (m, 12H), 1.75 (m, 24H), 1.85 (m, 24H), 2.48-2.61 (m, 60H), 3.16 (m, 42H), 4.57 (m, 12H), 4.84 (m, obscured by water peak, 9H), 6.58 (s, br, OC(O)NHCH_2), 6.70 (s, br, OC(O)NHCH_2). m/z (MALDI TOF (Voyager) MS) 3370.2 [$\text{M}+\text{Na}$] $^+$, 3386.1 [$\text{M}+\text{K}$] $^+$, calculated $M_w = 3345.23$. GPC; $M_w = 2780$, PDI = 1.05.

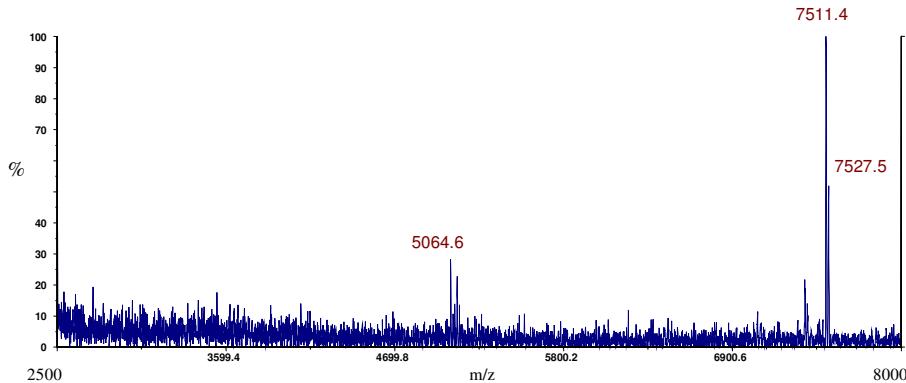
Synthesis of G3-4-heptyl Dendrimer TAEA:



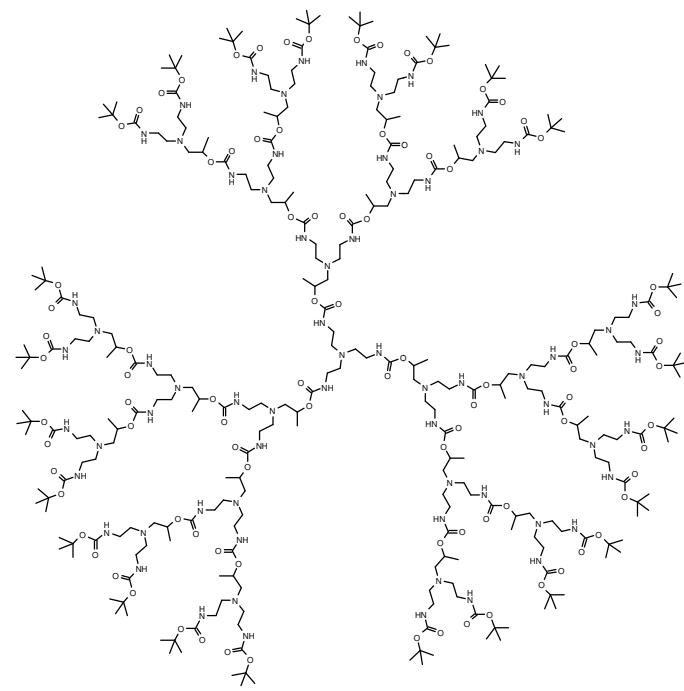
colourless oil obtained was purified further by preparative GPC (Biobeads, eluting with toluene) to give G3-4-heptyl Dendrimer TAEA as an extremely sticky oil (280 mg, 24%). $T_g = 19^\circ\text{C}$. Found C, 57.37; H, 9.50; N, 11.88%. $\text{C}_{366}\text{H}_{711}\text{O}_{90}\text{N}_{67}$ requires, C, 58.68; H, 9.57; N, 12.53%. ^{13}C NMR (100 MHz, CD_3OD) δ (ppm)= 14.6, 19.1, 19.7, 40.0, 40.1, 55.7, 61.0, 70.7, 75.2, 158.7, 158.8, 159.3. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 0.92 (t, $J=7.2\text{Hz}$, 144H), 1.20 (d, $J=6\text{Hz}$, 63H), 1.36 (m, 96H), 1.50 (m, 96H), 2.51-2.66 (m, 132H), 3.12-3.20 (m, 90H), 4.74 (m, 24H), 4.85 (m, obscured by water peak, 9H), 6.46 (s, br, OC(O)NHCH_2), 6.76 (s, br, OC(O)NHCH_2). m/z (MALDI TOF (Kratos) MS) 7511.4 [$\text{M}+\text{Na}^+$], 7527.5 [$\text{M}+\text{K}^+$], calculated $M_w = 7490.96$ and an impurity at 5063.6 corresponding to the two-armed dendrimer. GPC; $M_w = 6410$, PDI = 1.01.

CDI (92 mg, 0.57 mmol) was added to a stirred solution of **6a** (1.15 g, 0.47 mmol) in toluene (40 mL) and the mixture was heated at 60°C for 4 hours. Subsequently, the reaction mixture was analysed by ^1H NMR spectroscopy and interpretation of the spectrum indicated no evidence of the presence of starting materials. Tris(2-aminoethyl)amine (23 mg, 0.16 mmol) was added to the solution and the mixture was heated for 1 day at 60°C . The reaction mixture was concentrated *in vacuo* and redissolved in CH_2Cl_2 (100 mL). The organic phase was subsequently washed with water (3 x 100 mL), dried over MgSO_4 and the solvent removed using the rotary evaporator. The yellow oil obtained was purified by column chromatography (silica gel, eluting with EtOAc:MeOH 100:5 increasing to EtOAc:MeOH 100:10). The

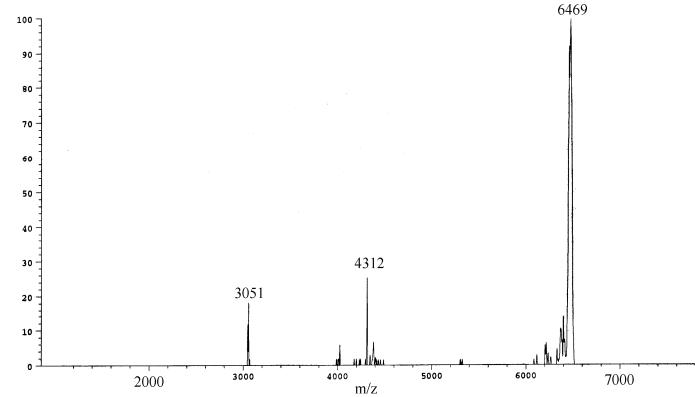
MALDI TOF – MS of G3-4-heptyl Dendrimer TAEA



Synthesis of G3-*t*-butyl Dendrimer TAEA:

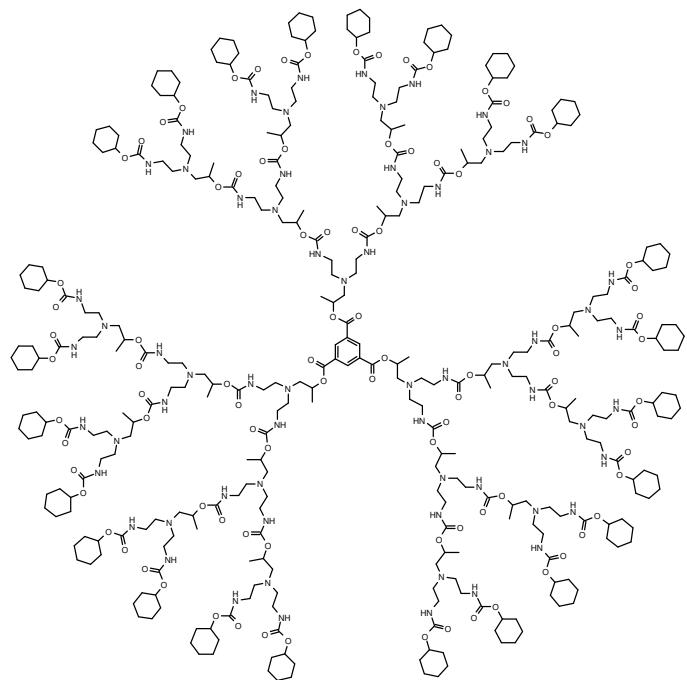


The procedure was similar to that described for the synthesis of G3-4-heptyl Dendrimer TAEA, but **6b** was used as the starting material. After the same purification method G3-*t*-butyl Dendrimer TAEA was isolated as a white amorphous solid (20%). $T_g = 49^\circ\text{C}$. Found C, 54.46; H, 8.74; N, 13.41%. $\text{C}_{294}\text{H}_{567}\text{O}_{90}\text{N}_{67}$ requires, C, 54.48; H, 8.82; N, 14.48%. ^{13}C NMR (125 MHz, CD_3OD) δ (ppm)= 19.1, 29.0, 39.9, 40.2, 55.6, 55.7, 61.1, 70.9, 80.0, 158.3, 158.6. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 1.20 (d, $J=6.4\text{Hz}$, 63H), 1.44 (s, 216H), 2.48-2.63 (m, 132H), 3.05-3.25 (m, 90H), 4.85 (m, obscured by water peak, 21H), 6.42 (s, br, OC(O)NHCH_2), 6.71 (s, br, OC(O)NHCH_2). m/z (ES MS) 3235.8 [$\text{M}+\text{H}]^{2+}$, 3246.9 [$\text{M}+\text{Na}]^{2+}$, 3257.9 [$\text{M}+2\text{Na}]^{2+}$. m/z (MALDI TOF (Kratos) MS) 6469 [$\text{M}+\text{H}]^+$, calculated $M_w = 6481.05$. GPC; $M_w = 4980$, PDI = 1.06.



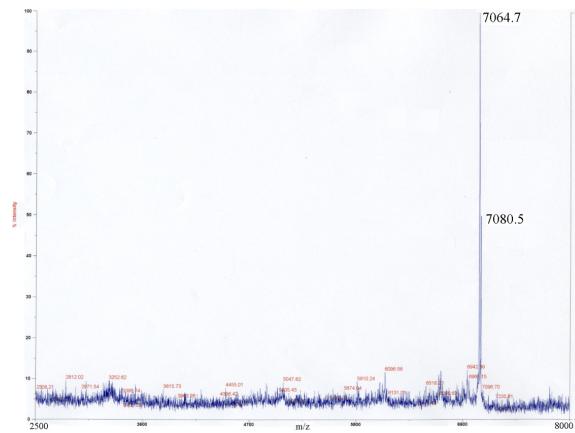
MALDI TOF-MS of G3-*t*-butyl Dendrimer TAEA

Synthesis of G3-cyclohexyl Dendrimer BTT:

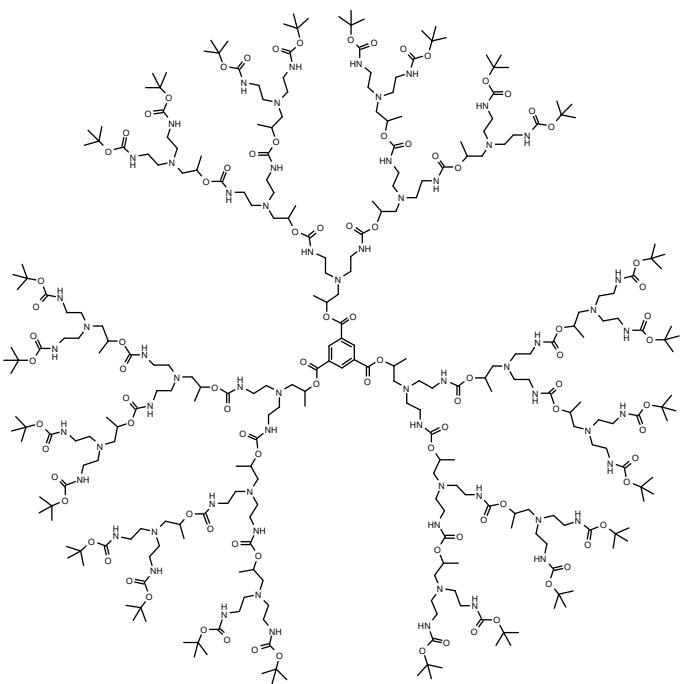


CD_3OD $\delta(\text{ppm}) = 18.9, 19.1, 24.9, 26.6, 33.2, 40.0, 40.5, 55.5, 55.8, 60.5, 61.0, 70.7, 72.3, 74.0, 133.1, 135.4, 158.6, 158.7, 158.8, 165.7$. ^1H NMR (400 MHz, CD_3OD) $\delta(\text{ppm}) = 1.19$ (d, $J=6\text{Hz}$, 54H), 1.24-1.41 (m, 129H), 1.55 (m, 24H), 1.73 (m, 48H), 1.84 (m, 48H), 2.48-2.86 (m, 126H), 3.10-3.26 (m, 84H), 4.56 (m, 24H), 4.86 (m, obscured by water peak, 18H), 5.28 (m, 3H), 6.58 (s, br, OC(O)NHCH_2), 6.71 (s, br, OC(O)NHCH_2), 8.81 (s, 3H). m/z (MALDI TOF (Voyager) MS) 7064.6 [$\text{M}+\text{Na}]^+$, 7080.5 [$\text{M}+\text{K}]^+$, calculated $M_w = 7037.82$. GPC; $M_w = 6410$, PDI = 1.01.

A solution of **6c** (0.64 g, 0.28 mmol) and DMAP (90 mg, 0.74 mmol) in benzene (50 mL) was refluxed for 4 hrs with a Dean-Stark trap filled with molecular sieves attached. The mixture was cooled to room temperature and 1,3,5-benzenetricarbonyl trichloride (22 mg, 8.29×10^{-2} mmol) was added. The reaction mixture was stirred and heated at reflux temperature (81°C) for 22 hrs and then concentrated *in vacuo*. The crude product was purified by column chromatography (silica gel, eluting with EtOAc:MeOH , 100:5) and by preparative GPC (Biobeads, eluting with toluene) to give G3-cyclohexyl Dendrimer BTT as a white amorphous solid (290 mg, 50%). $T_g = 50^\circ\text{C}$. Found C, 57.00; H, 8.52; N, 12.92%. $C_{342}\text{H}_{603}\text{O}_{90}\text{N}_{63}$ requires, C, 58.37; H, 8.64; N, 12.54%. ^{13}C NMR (100 MHz,



Synthesis of G3-*t*-butyl Dendrimer BTT:

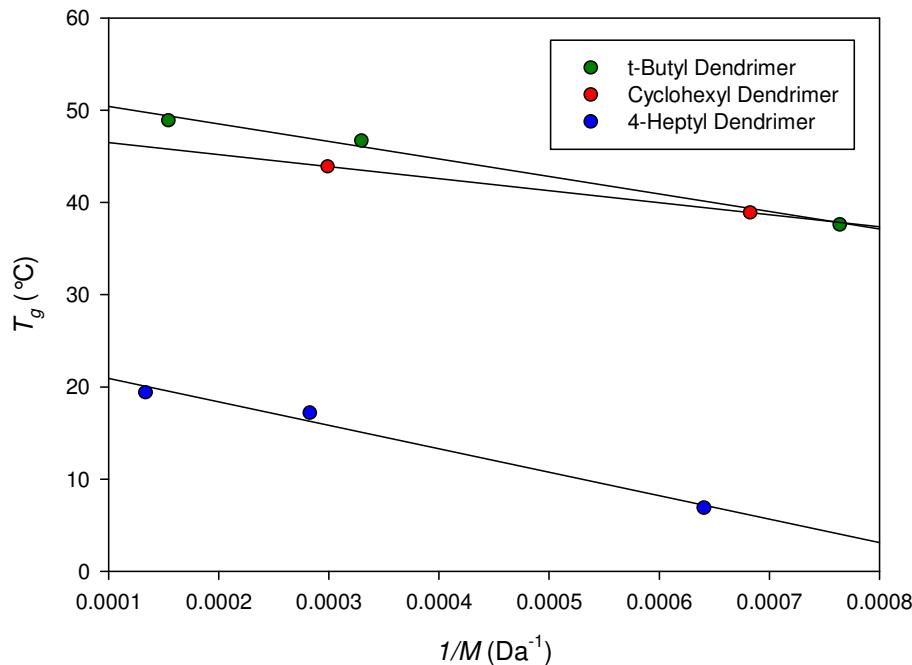


The procedure was similar to that described for the synthesis of G3-cyclohexyl Dendrimer BTT, but **6b** was used as the starting material. After the same purification method G3-*t*-butyl Dendrimer BTT was isolated as a white amorphous solid (48%). $T_g = 49^\circ\text{C}$. Found C, 55.17; H, 8.67; N, 12.52%. $C_{294}H_{555}O_{90}N_{63}$ requires, C, 55.06; H, 8.72; N, 13.76%. ^{13}C NMR (100 MHz, CD_3OD) δ (ppm)= 18.9, 19.1, 29.0, 30.9, 40.0, 40.1, 55.7, 61.0, 70.7, 72.3, 80.0, 133.1, 135.4, 158.4, 158.7, 158.8, 165.7. ^1H NMR (400 MHz, CD_3OD) δ (ppm)= 1.20 (d, 54H), 1.44 (m, 225H), 2.49-2.86 (m, 126H), 3.08-3.21 (m, 84H), 4.85 (m, obscured by water peak, 18H), 5.28 (m, 3H), 6.43 (s, br, OC(O)NHCH_2), 6.73 (s, br, OC(O)NHCH_2), 8.80 (s, 3H). GPC; $M_w = 5650$, calculated $M_w = 6412.92$, PDI = 1.03.

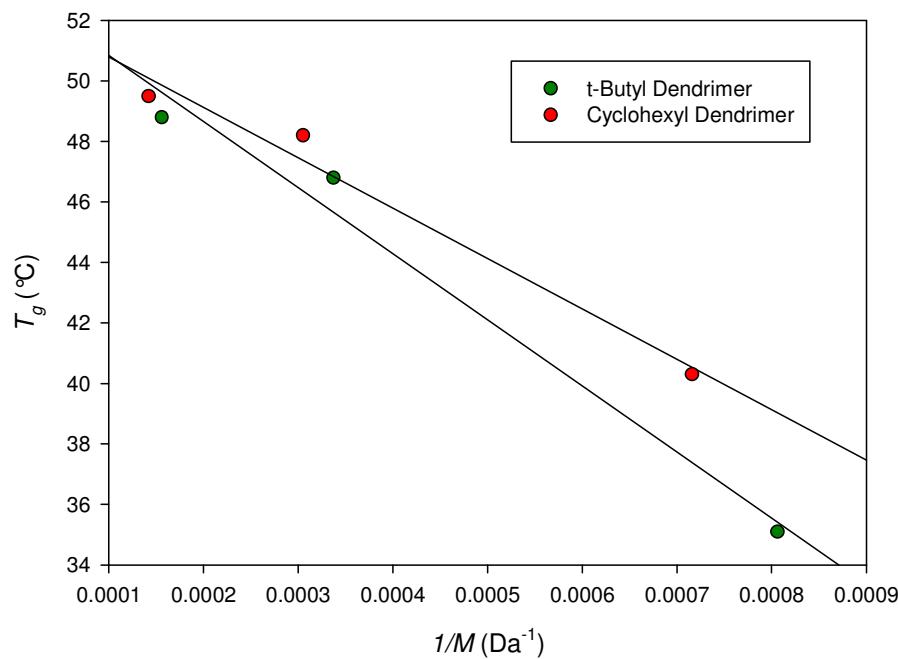
Graphical Analysis

Conventional Flory-Fox analysis

Dendrimers comprising TAEA cores

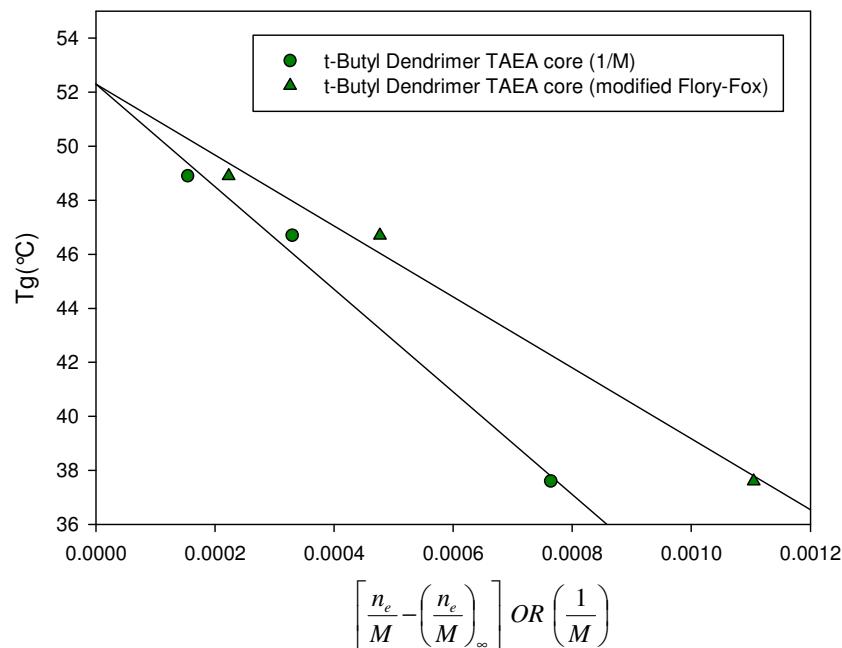


Dendrimers comprising BTT cores

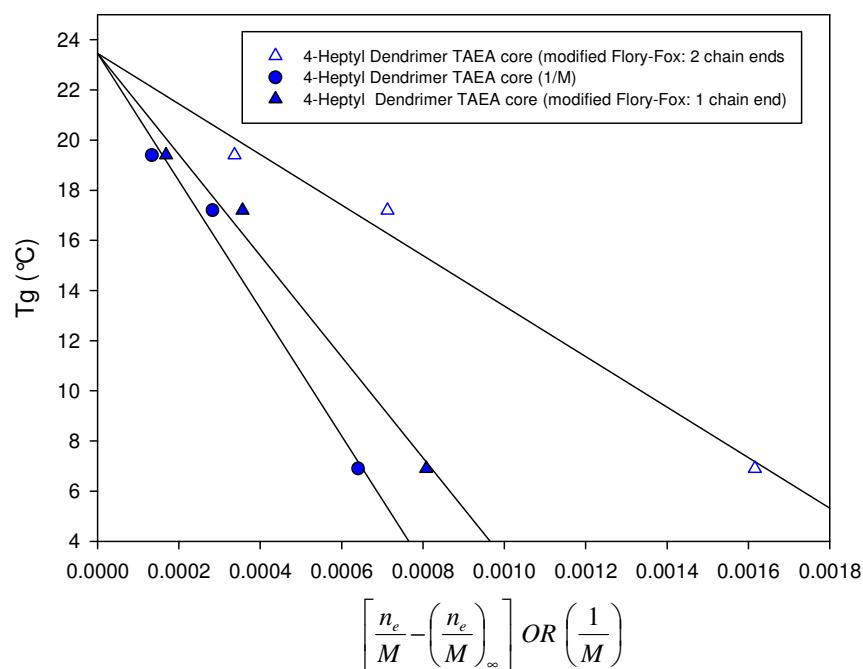


Comparison of modified Flory-Fox vs Flory-Fox analysis

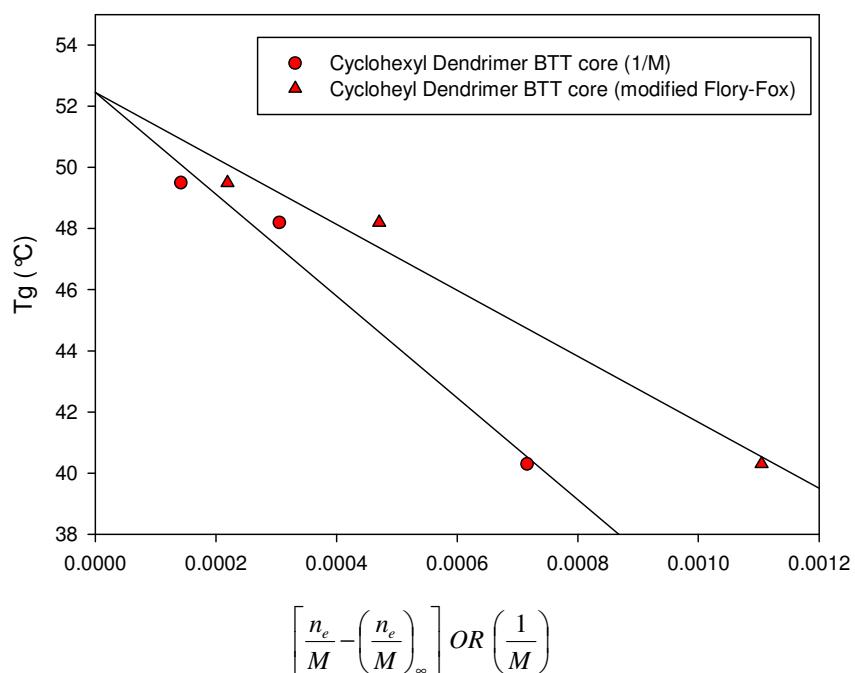
Dendrimers comprising TAEA cores and *t*-butyl surface functionality



Dendrimers comprising TAEA cores and 4-heptyl surface functionality



Dendrimers comprising BTT cores and cyclohexyl surface functionality



Example calculations of $(ne/M)_\infty$

Cyclohexyl functional dendrons (GREY = experimental data, blue = $(ne/M)_\infty$ values)

| Generation | Molecular Weight | number of end groups (ne) | ne/M | ne/M – $(ne/M)_\infty$ |
|------------|------------------|---------------------------|-------------|------------------------|
| 1 | 413.56 | 2 | 4.83610E-03 | 1.65E-03 |
| 2 | 1040.36 | 4 | 3.84480E-03 | 6.54E-04 |
| 3 | 2293.96 | 8 | 3.48740E-03 | 2.97E-04 |
| 4 | 4801.16 | 16 | 3.33250E-03 | 1.42E-04 |
| 5 | 9815.56 | 32 | 3.26010E-03 | |
| 6 | 19844.36 | 64 | 3.22510E-03 | |
| 7 | 39901.96 | 128 | 3.20790E-03 | |
| 8 | 80017.16 | 256 | 3.19930E-03 | |
| 9 | 160247.56 | 512 | 3.19510E-03 | |
| 10 | 320708.36 | 1024 | 3.19290E-03 | |
| 11 | 641629.96 | 2048 | 3.19190E-03 | |
| 12 | 1283473.16 | 4096 | 3.19130E-03 | |
| 13 | 2567159.56 | 8192 | 3.19110E-03 | |
| 14 | 5134532.36 | 16384 | 3.19090E-03 | |
| 15 | 10269277.96 | 32768 | 3.19090E-03 | |
| 16 | 20538769.16 | 65536 | 3.19080E-03 | |
| 17 | 41077751.56 | 131072 | 3.19080E-03 | |
| 18 | 82155716.36 | 262144 | 3.19080E-03 | |
| 19 | 164311646 | 524288 | 3.19080E-03 | |
| 20 | 328623505.2 | 1048576 | 3.19080E-03 | |
| 21 | 657247223.6 | 2097152 | 3.19080E-03 | |
| 22 | 1314494660 | 4194304 | 3.19080E-03 | |
| 23 | 2628989534 | 8388608 | 3.19080E-03 | |
| 24 | 5257979281 | 16777216 | 3.19080E-03 | |
| 25 | 10515958776 | 33554432 | 3.19080E-03 | |
| 26 | 21031917764 | 67108864 | 3.19080E-03 | |
| 27 | 42063835742 | 134217728 | 3.19080E-03 | |
| 28 | 84127671697 | 268435456 | 3.19080E-03 | |
| 29 | 1.68255E+11 | 536870912 | 3.19080E-03 | |
| 30 | 3.36511E+11 | 1073741824 | 3.19080E-03 | |

4-Heptyl functional TAEA Dendrimers (GREY = experimental data, blue = $(ne/M)^\infty$ values)

| Generation | Molecular Weight | number of end groups (ne) | ne/M | ne/M – $(ne/M)^\infty$ |
|------------|------------------|---------------------------|-------------|------------------------|
| 1 | 1561.17 | 6 | 3.84330E-03 | 8.08E-04 |
| 2 | 3537.82 | 12 | 3.39190E-03 | 3.56E-04 |
| 3 | 7491.14 | 24 | 3.20380E-03 | 1.68E-04 |
| 4 | 15397.77 | 48 | 3.11730E-03 | |
| 5 | 31211.03 | 96 | 3.07580E-03 | |
| 6 | 62837.55 | 192 | 3.05550E-03 | |
| 7 | 126090.59 | 384 | 3.04540E-03 | |
| 8 | 252596.67 | 768 | 3.04040E-03 | |
| 9 | 505608.83 | 1536 | 3.03790E-03 | |
| 10 | 1011633.15 | 3072 | 3.03670E-03 | |
| 11 | 2023681.79 | 6144 | 3.03610E-03 | |
| 12 | 4047779.07 | 12288 | 3.03570E-03 | |
| 13 | 8095973.63 | 24576 | 3.03560E-03 | |
| 14 | 16192362.75 | 49152 | 3.03550E-03 | |
| 15 | 32385140.99 | 98304 | 3.03550E-03 | |
| 16 | 64770697.47 | 196608 | 3.03540E-03 | |
| 17 | 129541810.4 | 393216 | 3.03540E-03 | |
| 18 | 259084036.4 | 786432 | 3.03540E-03 | |
| 19 | 518168488.2 | 1572864 | 3.03540E-03 | |
| 20 | 1036337392 | 3145728 | 3.03540E-03 | |
| 21 | 2072675199 | 6291456 | 3.03540E-03 | |
| 22 | 4145350814 | 12582912 | 3.03540E-03 | |
| 23 | 8290702043 | 25165824 | 3.03540E-03 | |
| 24 | 16581404502 | 50331648 | 3.03540E-03 | |
| 25 | 33162809420 | 100663296 | 3.03540E-03 | |
| 26 | 66325619256 | 201326592 | 3.03540E-03 | |
| 27 | 1.32651E+11 | 402653184 | 3.03540E-03 | |
| 28 | 2.65302E+11 | 805306368 | 3.03540E-03 | |
| 29 | 5.30605E+11 | 1610612736 | 3.03540E-03 | |
| 30 | 1.06121E+12 | 3221225472 | 3.03540E-03 | |

t-Butyl functional BTT Dendrimers (GREY = experimental data, blue = $(ne/M)_{\infty}$ values)

| Generation | Molecular Weight | number of end groups (ne) | ne/M | ne/M – $(ne/M)_{\infty}$ |
|------------|------------------|---------------------------|-------------|--------------------------|
| 1 | 1240.56 | 6 | 4.83650E-03 | 1.36E-03 |
| 2 | 2964.73 | 12 | 4.04760E-03 | 5.68E-04 |
| 3 | 6413.07 | 24 | 3.74240E-03 | 2.62E-04 |
| 4 | 13309.75 | 48 | 3.60640E-03 | |
| 5 | 27103.11 | 96 | 3.54200E-03 | |
| 6 | 54689.83 | 192 | 3.51070E-03 | |
| 7 | 109863.27 | 384 | 3.49530E-03 | |
| 8 | 220210.15 | 768 | 3.48760E-03 | |
| 9 | 440903.91 | 1536 | 3.48380E-03 | |
| 10 | 882291.43 | 3072 | 3.48180E-03 | |
| 11 | 1765066.47 | 6144 | 3.48090E-03 | |
| 12 | 3530616.55 | 12288 | 3.48040E-03 | |
| 13 | 7061716.71 | 24576 | 3.48020E-03 | |
| 14 | 14123917.03 | 49152 | 3.48010E-03 | |
| 15 | 28248317.67 | 98304 | 3.48000E-03 | |
| 16 | 56497118.95 | 196608 | 3.48000E-03 | |
| 17 | 112994721.5 | 393216 | 3.48000E-03 | |
| 18 | 225989926.6 | 786432 | 3.47990E-03 | |
| 19 | 451980336.9 | 1572864 | 3.47990E-03 | |
| 20 | 903961157.4 | 3145728 | 3.47990E-03 | |
| 21 | 1807922798 | 6291456 | 3.47990E-03 | |
| 22 | 3615846080 | 12582912 | 3.47990E-03 | |
| 23 | 7231692644 | 25165824 | 3.47990E-03 | |
| 24 | 14463385772 | 50331648 | 3.47990E-03 | |
| 25 | 28926772027 | 100663296 | 3.47990E-03 | |
| 26 | 57853544538 | 201326592 | 3.47990E-03 | |
| 27 | 1.15707E+11 | 402653184 | 3.47990E-03 | |
| 28 | 2.31414E+11 | 805306368 | 3.47990E-03 | |
| 29 | 4.62828E+11 | 1610612736 | 3.47990E-03 | |
| 30 | 9.25657E+11 | 3221225472 | 3.47990E-03 | |

Analysis of Wooley *et al*¹ data and comparison of geometric progression, Flory-Fox and modified Flory-Fox approaches

| | Tg (K) | M | 1/M | n _e | n _e /M | (n _e /M)-(n _e /M) _∞ | 2 ^{Gn} | 2 ^{Gn} C ² | 1/(2 ^{Gn} C ² -CA) |
|---------|--------|-------|---------|----------------|-------------------|--|-----------------|--------------------------------|--|
| [G1]-OH | 255 | 320 | 0.00313 | 3 | 0.00938 | 0.004658 | 2 | 89888 | 1.47406x10 ⁻⁵ |
| [G2]-OH | 285 | 744 | 0.00134 | 5 | 0.00672 | 0.002003 | 4 | 179776 | 6.34003x10 ⁻⁶ |
| [G3]-OH | 305 | 1592 | 0.00063 | 9 | 0.00565 | 0.000936 | 8 | 359552 | 2.96293x10 ⁻⁶ |
| [G4]-OH | 312 | 3288 | 0.0003 | 17 | 0.00517 | 0.000453 | 16 | 719104 | 1.4346x10 ⁻⁶ |
| [G5]-OH | 315 | 6680 | 0.00015 | 33 | 0.00494 | 0.000223 | 32 | 1438208 | 7.06135x10 ⁻⁷ |
| [G6]-OH | 316 | 13464 | 7.4E-05 | 65 | 0.00483 | 0.000111 | 64 | 2876416 | 3.5034x10 ⁻⁷ |

The polybenzylether dendrons exhibit a geometric progression of molecular weight that is described by the equation 5 (see manuscript)

$$M_{Gn} = 2(M_{Gn-1}) + A$$

The factor A can therefore be determined as A = 104Da

The factor B is determined by equation 6 (see manuscript) as the generation 1 molecular weight minus the factor A, ie

$$B = M_{G1} - A$$

B is readily determined to be B = 320 - A = 216 Da

Using equation 8 (see manuscript) it is possible to determine the molecular weight of any generation *n*.

$$M_{Gn} = B2^{Gn-1} + A2^{Gn} - A$$

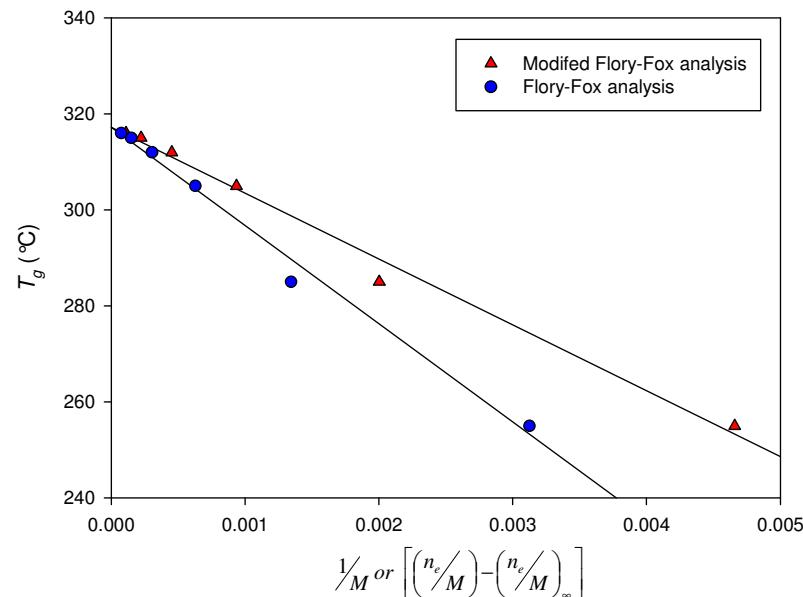
eg Generation 6 = 216(2⁵) + 104(2⁶) - 104 = 6912 + 6656 - 104 = 13464 Da

Factor C is defined a C=B/2+A and is therefore C = 212 Da

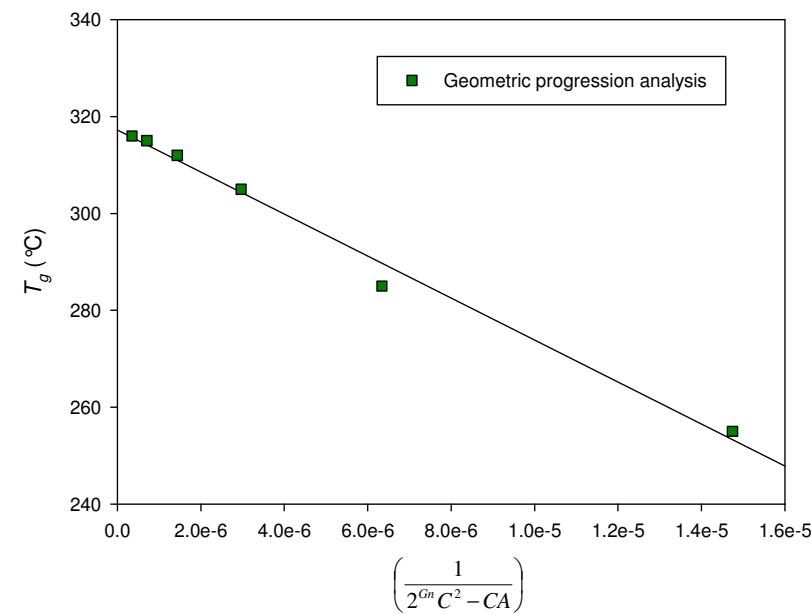
With these values (A = 104 Da; B = 216 Da; C = 212 Da), equation 18 (see manuscript) may be used to determine T_{g∞} through a plot of T_{g,Gn} vs. 1/(2^{Gn}C²-CA).

$$T_{g,Gn} = T_{g∞} - K \left(\frac{1}{2^{Gn} C^2 - CA} \right)$$

Comparative graphs for the dendrons of the Wooley *et al*¹ paper are shown below.



Calculated $T_{g\infty}$ values: Flory-Fox analysis gives 317.17072K; Modified Flory-Fox analysis gives 317.16857K.



Calculated $T_{g\infty}$ values: Geometric progression analysis gives 317.17072K.

Data for all materials described in Wooley *et al*¹ report with calculations for geometric progression analysis

| Generation | Surface | MW ^b | 2^{Gn} | A | B | C | $\frac{1}{(2^{Gn}C^2 - CA)}$ | 1/M | (ne/M) - (ne/M) _∞ | Tg (K) |
|------------|------------------|------------------|----------|-----|-----|-----|------------------------------|-----------------------|------------------------------|--------|
| 1 | H | 320 | 2 | 104 | 216 | 212 | 1.47×10^{-5} | 3.13×10^{-3} | 4.66×10^{-3} | 255 |
| 2 | H | 744 | 4 | 104 | 216 | 212 | 6.34×10^{-6} | 1.34×10^{-3} | 2.00×10^{-3} | 285 |
| 3 | H | 1592 | 8 | 104 | 216 | 212 | 2.96×10^{-6} | 6.28×10^{-4} | 9.36×10^{-4} | 305 |
| 4 | H | 3288 | 16 | 104 | 216 | 212 | 1.43×10^{-6} | 3.04×10^{-4} | 4.53×10^{-4} | 312 |
| 5 | H | 6680 | 32 | 104 | 216 | 212 | 7.06×10^{-7} | 1.50×10^{-4} | 2.23×10^{-4} | 315 |
| 6 | H | 13464 | 64 | 104 | 216 | 212 | 3.50×10^{-7} | 7.43×10^{-5} | 1.11×10^{-4} | 316 |
| 1 | Br | 478 | 2 | 104 | 374 | 291 | 7.19×10^{-6} | 2.09×10^{-3} | 2.84×10^{-3} | 271 |
| 2 | Br | 1060 | 4 | 104 | 374 | 291 | 3.24×10^{-6} | 9.43×10^{-4} | 1.28×10^{-3} | 309 |
| 3 | Br | 2224 | 8 | 104 | 374 | 291 | 1.55×10^{-6} | 4.50×10^{-4} | 6.10×10^{-4} | 316 |
| 4 | Br | 4552 | 16 | 104 | 374 | 291 | 7.55×10^{-7} | 2.20×10^{-4} | 2.98×10^{-4} | 325 |
| 1 | CN | 370 | 2 | 104 | 266 | 237 | 1.14×10^{-5} | 2.70×10^{-3} | 3.89×10^{-3} | 287 |
| 2 | CN | 844 | 4 | 104 | 266 | 237 | 5.00×10^{-6} | 1.18×10^{-3} | 1.70×10^{-3} | 327 |
| 3 | CN | 1792 | 8 | 104 | 266 | 237 | 2.35×10^{-6} | 5.58×10^{-4} | 8.03×10^{-4} | 334 |
| 4 | CN | 3688 | 16 | 104 | 266 | 237 | 1.14×10^{-6} | 2.71×10^{-4} | 3.90×10^{-4} | 349 |
| 1 | C-2 ^a | 366 ^a | 2 | 58 | 308 | 212 | 1.29×10^{-5} | 2.73×10^{-3} | 7.47×10^{-4} | 270 |
| 2 | C-2 | 790 | 4 | 58 | 308 | 212 | 5.97×10^{-6} | 1.27×10^{-3} | 3.46×10^{-4} | 287 |
| 3 | C-2 | 1656 (1638) | 8 | 58 | 308 | 212 | 2.88×10^{-6} | 6.11×10^{-4} | 1.67×10^{-4} | 306 |
| 4 | C-2 | 3354 (3334) | 16 | 58 | 308 | 212 | 1.41×10^{-6} | 3.00×10^{-4} | 8.20×10^{-5} | 311 |
| 5 | C-2 | 6750 (6726) | 32 | 58 | 308 | 212 | 7.01×10^{-7} | 1.49×10^{-4} | 4.07×10^{-5} | 311 |
| 6 | C-2 | 13542 (13510) | 64 | 58 | 308 | 212 | 3.49×10^{-7} | 7.40×10^{-5} | 2.02×10^{-5} | 312 |
| 1 | C-3 | 576 | 2 | 60 | 516 | 318 | 5.46×10^{-6} | 1.74×10^{-3} | 4.90×10^{-4} | 282 |
| 2 | C-3 | 1212 | 4 | 60 | 516 | 318 | 2.59×10^{-6} | 8.25×10^{-4} | 2.32×10^{-4} | 298 |
| 3 | C-3 | 2484 | 8 | 60 | 516 | 318 | 1.27×10^{-6} | 4.03×10^{-4} | 1.12×10^{-4} | 309 |
| 4 | C-3 | 5026 | 16 | 60 | 516 | 318 | 6.25×10^{-7} | 1.99×10^{-4} | 5.63×10^{-5} | 312 |
| 5 | C-3 | 10126 | 32 | 60 | 516 | 318 | 3.11×10^{-7} | 9.89×10^{-5} | 2.80×10^{-5} | 314 |
| 6 | C-3 | 20292 | 64 | 60 | 516 | 318 | 1.55×10^{-7} | 4.93×10^{-5} | 1.40×10^{-5} | 315 |
| 1 | C-OH | 714 | 2 | 102 | 612 | 408 | 3.43×10^{-6} | 1.40×10^{-3} | 1.05×10^{-3} | 446 |
| 2 | C-OH | 1530 | 4 | 102 | 612 | 408 | 1.60×10^{-6} | 6.54×10^{-4} | 4.90×10^{-4} | 458 |
| 3 | C-OH | 3162 | 8 | 102 | 612 | 408 | 7.75×10^{-7} | 3.16×10^{-4} | 2.37×10^{-4} | 467 |
| 4 | C-OH | 6426 | 16 | 102 | 612 | 408 | 3.81×10^{-7} | 1.56×10^{-4} | 1.17×10^{-4} | 474 |

^aThis molecule is a core rather than a dendrimer

^bValues in brackets are corrected molecular weights; values without brackets are molecular weights reported from measurement

¹K. L. Wooley, C. J. Hawker, J. M. Pochan and J. M. J. Fréchet, Macromolecules, 1993, **26**, 1514.