# Supplementary figures to "Yielding dynamics of a Herschel-Bulkley fluid: a critical-like fluidization behaviour"

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#### **1** Supplementary Figure 1

The total slip velocity  $v_s$  was computed as the sum of slip velocities at the rotor and at the stator recorded once steady state is reached and averaged over at least 150 s. Supplementary Figure 1 shows  $v_s$  relative to the rotor velocity  $v_0$  for various gap widths and applied shear rates.  $v_s/v_0$  is much larger for small gap widths than for larger gaps. For e = 0.45 mm, the amount of wall slip is about 30 %, independent of or weakly decreasing with  $\dot{\gamma}$ . The same trend is observed for e = 1.5 mm yet wall slip is smaller and of the order of 15 %. For e = 3 mm however, the relative slip sharply decreases with  $\dot{\gamma}$  from about 20 % at the lowest shear rate down to negligible values of the order of our uncertainty of about 2 %.



**Fig. 1** Steady-state total slip velocity  $v_s$  relative to the rotor velocity  $v_0$  as a function of the applied shear rate  $\dot{\gamma}$  for smooth Couette geometries of gap width  $e = 0.45 \text{ mm} (\Box)$ ,  $e = 1.5 \text{ mm} (\diamondsuit)$ , and  $e = 3 \text{ mm} (\bullet)$ . Dotted lines are power laws drawn to guide the eye. Experiments performed on different batches of 1 % w/w carbopol microgels.

### 2 Supplementary Figure 2

Supplementary Figure 2 shows the spatiotemporal diagrams of v(x,t) recorded in the three different Couette cells for similar shear rates  $\dot{\gamma} \simeq 0.8 \text{ s}^{-1}$  together with the corresponding stress responses. Transient shear banding is observed for  $t < \tau_f$  as indicated by white dotted lines (see also the movies in the supplementary material<sup>†</sup>).

The results for e = 0.45 mm are qualitatively similar to those found previously for e = 1 mm and  $\dot{\gamma} < \dot{\gamma}^*$  [see e.g.

 $\dot{\gamma} = 1.5 \text{ s}^{-1}$  in Fig. 9(a)], i.e. the transient regime presents a quasi-stationary phase followed by strong fluctuations and abrupt full fluidization. Here, it is interesting to note that the quasi-stationary phase ( $t \leq 10^3$  s) involves a pluglike flow at about half the rotor velocity whose velocity slowly decreases and that precedes the nucleation of a fluctuating shear band (see also the movie in the supplementary material<sup>†</sup>). This initial plug flow is only seen in smooth geometries and was already evidenced in a previous study devoted to the stress overshoot phenomenon at short times.<sup>1</sup>

On the other hand, the spatiotemporal diagrams for e = 1.5 mm and e = 3 mm resemble that of Fig. 9(c). Indeed, as the gap width is increased, the characteristic kink in  $\sigma(t)$  disappears as well as the fluctuations of the flow field, and the shear banding regime becomes more progressive and continuous.

#### References

1 T. Divoux, C. Barentin and S. Manneville, <u>Soft Matter</u>, 2011, 7, 9335– 9349.



Fig. 2 Spatiotemporal diagrams of the velocity data v(r,t) in smooth Couette cells of different gap widths *e* and under similar shear rates. (a) e = 0.45 mm and  $\dot{\gamma} = 0.85$  s<sup>-1</sup>. (b) e = 1.5 mm and  $\dot{\gamma} = 0.8$  s<sup>-1</sup>. (c) e = 3 mm and  $\dot{\gamma} = 0.7$  s<sup>-1</sup>. White lines are the corresponding stress responses  $\sigma(t)$  (right vertical axis). The vertical dashed lines indicate the fluidization times  $\tau_f$ . The time interval between two velocity profiles is 21 s, 17 s, and 4 s in (a), (b), and (c) respectively.