

Supplementary Material for “**Elastic nanomembrane metrology at fluid/fluid interfaces using axisymmetric drop shape analysis with anisotropic surface tensions: deviations from Young-Laplace equation**” by James K. Ferri et al.

Isotropic Interfacial tension and Flat Disc Membrane.

Figure S1 compares the shapes calculated by equations (2) and (3), the Young-Laplace equation, and equations (5) and (6), the anisotropic surface stress equations, which are identical.

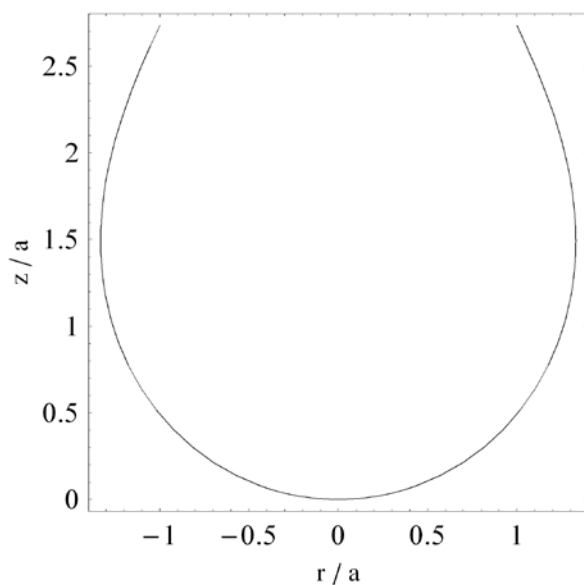


Figure S1. No deformation; linear elastic interface equation (4a). $\lambda_1=\lambda_2=1$; $G_s=100$ mN/m; $\nu_s=0$; $R_0=1320 \text{ m}^{-1}$; $\Delta\rho=997 \text{ kg m}^{-3}$; $\gamma(\Gamma)=50 \text{ mN/m}$.

Linear elastic nanomembranes at axisymmetric fluid/fluid interfaces: effect of surface shear modulus on surface deformation.

From Figure S2, it is seen that the meridional stretching (λ_l) is maximum at the drop apex and that as the surface shear modulus increases, non-monotonic behavior develops in (λ_2). However, in all cases, the magnitude of the stretches is similar.

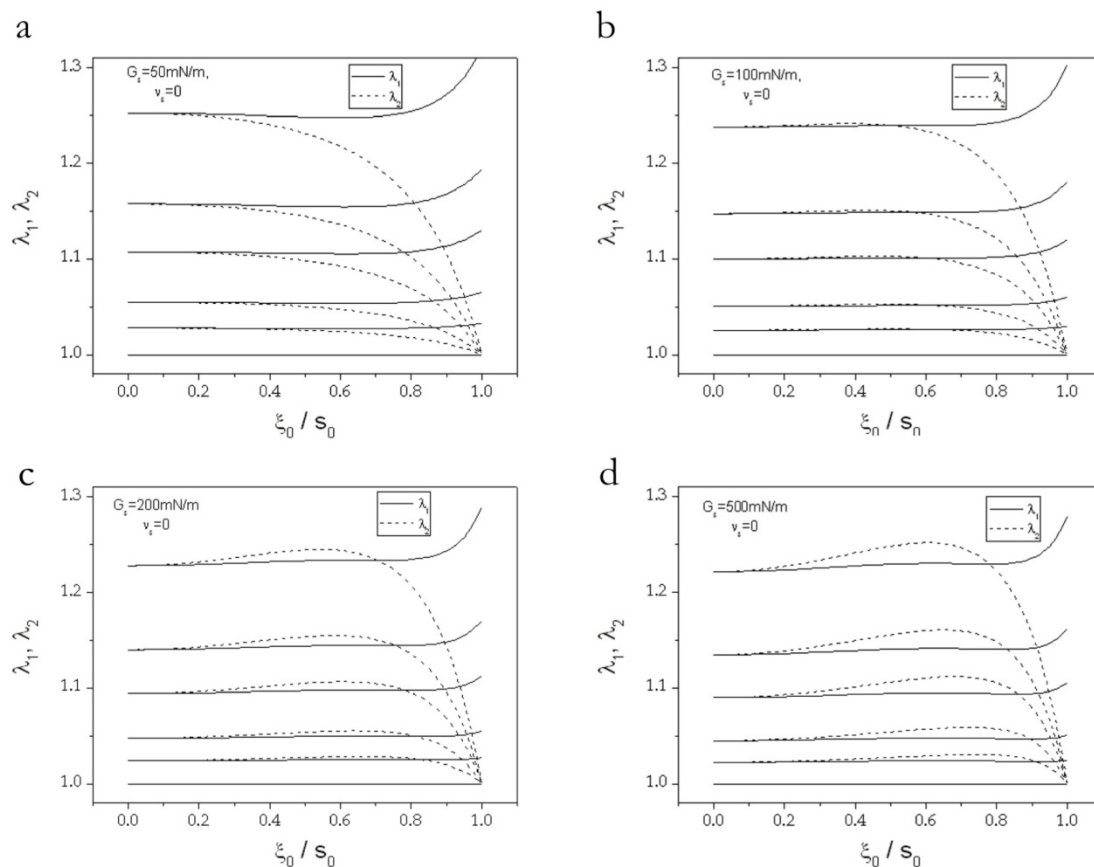


Figure S2. Effect of surface shear modulus on principal stretches, λ_1 (—) and λ_2 (---): G_s = (a) 50, (b) 100, (c) 200, (d) 500 mN/m, $v_s = 0$; for all calculations $\alpha = 0, 0.1, 0.2, 0.3, 0.4$ and 0.5 . $R_0 = 1320 \text{ m}^{-1}$, $\Delta\rho = 997 \text{ kgm}^{-3}$, $\gamma(T) = 50 \text{ mN/m}$.

Shape differences between surfaces with anisotropic stresses and the Young-Laplace equation.

Figure S3 shows the sum of the radial error as a function of inflation for different surface Poisson ratios. The figure confirms that the error, which results from using the Young-Laplace equation to describe an anisotropic surface, increases with increasing incompressibility (i.e. a greater value of ν_s). Although these errors are small in magnitude, it is clear that they are systematic, demonstrating the inherent deviations between the Young-Laplace equation and the case of anisotropic stress distributions.

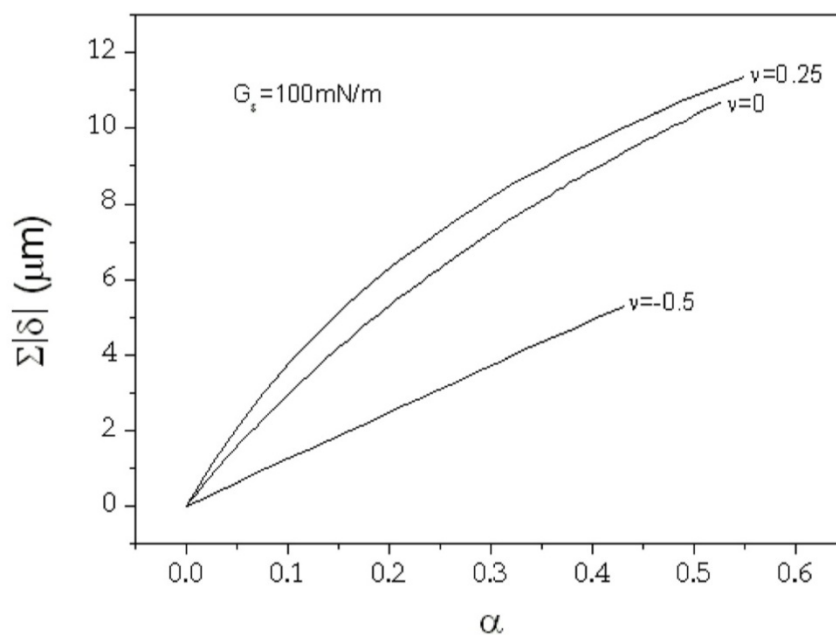


Figure S3. Sum of Young-Laplace error as a function of the surface Poisson ratio of the membrane, ν_s ; $G_s = 100 \text{ mN/m}$, $\nu_s = -0.5, 0, 0.25$.