

# Electronic Supplementary Information for Correlation between structure and mixed ionic–electronic conduction mechanism for $(La_{1-x}Sr_x)CoO_{3-\delta}$ using synchrotron X-ray analysis and first principle calculations

Takanori Itoh,<sup>\*a</sup> Manabu Inukai,<sup>b</sup> Naoto Kitamura,<sup>a</sup> Naoya Ishida,<sup>a</sup> Yasushi Idemoto,<sup>a</sup> Takashi Yamamoto,<sup>c</sup>

<sup>a</sup> Department of Pure and Applied Chemistry, Faculty of Science and Technology, Tokyo University of Science, Noda, Chiba 278-8510, Japan

\*Corresponding author: Fax: +81 299 84 0217; Tel: +81 299 84 0808; E-mail: takanori.itoh@agc.com

<sup>b</sup> Department of Material Science and Engineering, Faculty of Engineering, Nagoya Institute of Technology, Gokiso-cho, Showa-ku, Nagoya 466-8555, Japan.

<sup>c</sup> Department of Mathematical and Material Sciences, Faculty of Integrated Arts and Sciences, The University of Tokushima, Tokushima 770-8502, Japan.

Table S1 First principle calculation conditions for estimating band structure

Parameters	Fig.12 (a)	Fig.12 (b)	Fig.12 (c)	Fig.12 (d)	Fig.12 (e)	Fig.12 (f)
Lattice parameters of $a$ and $b$ -axis (Å)	5.44110	5.44511	5.42491	5.44110	5.44511	5.42491
Lattice parameter of $c$ -axis (Å)	13.08837	13.18596	13.22622	13.08837	13.18596	13.22622
$x$ of oxygen site	0.4496	0.4598	0.4742	0.4496	0.4496	0.4496

Table S2 First principle calculation conditions for estimating activation energies of oxygen diffusion

Parameters	○	●	△	▲
Lattice parameters of $a$ and $b$ -axis ( $\text{\AA}$ )	5.44110 ( $x = 0.00$ ), 5.44511 ( $x = 0.25$ ), 5.42491 ( $x = 0.50$ )	5.44511 ( $x = 0.0, 0.25, 0.50$ )	5.44110 ( $x = 0.00$ ), 5.44511 ( $x = 0.25$ ), 5.42491 ( $x = 0.50$ )	5.44110 ( $x = 0.0, 0.25, 0.50$ )
Lattice parameter of $c$ -axis ( $\text{\AA}$ )	13.08837 ( $x = 0.00$ ), 13.18596 ( $x = 0.25$ ), 13.22622 ( $x = 0.50$ )	13.18596 ( $x = 0.0, 0.25, 0.50$ )	13.08837 ( $x = 0.00$ ), 13.18596 ( $x = 0.25$ ), 13.22622 ( $x = 0.50$ )	13.08837 ( $x = 0.0, 0.25, 0.50$ )
$x(\text{O})$ of oxygen site	0.4496 ( $x = 0.00$ ), 0.4598 ( $x = 0.25$ ), 0.4496 ( $x = 0.50$ )	0.4496 ( $x = 0.00$ ), 0.4598 ( $x = 0.25$ ), 0.4496 ( $x = 0.50$ )	0.4496 ( $x = 0.0, 0.25, 0.50$ )	0.4496 ( $x = 0.0, 0.25, 0.50$ )
La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site	La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : La	La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : La	La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : La	La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : La, ( $x = 0.00$ ) La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : Sr, La, La ( $x = 0.167$ ) La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : Sr, Sr, La ( $x = 0.333$ ) La <sub>1</sub> , La <sub>2</sub> , La <sub>3</sub> site : Sr ( $x = 0.50$ )

Note:  $x(\text{O})$  : the oxide ion site fractional coordinate.

Table S3 Positional parameters for (La<sub>1-x</sub>Sr<sub>x</sub>)CoO<sub>3- $\delta$</sub>  in Rietveld refinements

Space group $R\bar{3}c$ setting 1 (No. 167) $\alpha = \beta = 90^\circ, \gamma = 120^\circ$			
Atoms	Sites	Site occupancy	Atomic coordinates
La, Sr	6a	1	0, 0, $\frac{1}{4}$
Co	6b	1	0, 0, 0
O	18e	$g(\text{O}) \sim 1$	$x \sim 0.5, 0, \frac{1}{4}$

Note:  $g(\text{O})$  : the oxide ion site occupancy calculated from Co valence estimated by potentiometric-titration.

Table S4 Structural parameters and reliability factors of  $(La_{1-x}Sr_x)CoO_{3-\delta}$  between  $x = 0.00$  and  $0.50$  from Rietveld refinements

Sites	Parameters	$x = 0$	$x = 0.05$	$x = 0.10$	$x = 0.15$	$x = 0.20$	$x = 0.25$	$x = 0.30$	$x = 0.35$	$x = 0.40$	$x = 0.45$	$x = 0.50$
La, Sr (6a)	$U_{11}, U_{22} (\text{\AA}^2)$	0.00386(9)	0.00387(10)	0.00489(9)	0.00431(8)	0.00445(8)	0.00449(9)	0.00448(9)	0.00464(10)	0.00459(10)	0.00449(9)	0.00454(9)
	$U_{33} (\text{\AA}^2)$	0.00436(8)	0.00434(9)	0.00455(8)	0.00445(9)	0.00439(9)	0.00431(9)	0.00431(9)	0.00458(10)	0.00460(9)	0.00469(9)	0.00455(8)
	$U_{12} (\text{\AA}^2)$	0.0025(2)	0.0025(2)	0.0026(2)	0.0028(2)	0.0027(2)	0.0027(2)	0.0028(2)	0.0028(2)	0.0029(2)	0.0029(2)	0.0028(2)
	$U_{13} U_{23} (\text{\AA}^2)$	0.0000(2)	0.0000(3)	0.0001(2)	0.0000(2)	-0.00001(2)	-0.0001(2)	-0.0002(2)	0.0000(3)	-0.0002(3)	-0.0003(2)	-0.0003(2)
Co (6b)	$U_{11}, U_{22} (\text{\AA}^2)$	0.00253(9)	0.0026(10)	0.00323(9)	0.00292(10)	0.00314(9)	0.00302(10)	0.00304(10)	0.00298(9)	0.00300(10)	0.00303(10)	0.00301(9)
	$U_{33} (\text{\AA}^2)$	0.00317(9)	0.00323(10)	0.00360(9)	0.00325(10)	0.00303(8)	0.00302(10)	0.00299(10)	0.00287(9)	0.00290(10)	0.00292(10)	0.00291(8)
	$U_{12} (\text{\AA}^2)$	0.00123(9)	0.00131(10)	0.00145(8)	0.00159(10)	0.00151(9)	0.00159(10)	0.00154(10)	0.00153(9)	0.00170(10)	0.00159(10)	0.00154(9)
	$U_{13} U_{23} (\text{\AA}^2)$	-0.0010(4)	-0.0012(5)	-0.0012(5)	-0.0005(6)	-0.0007(5)	-0.0005(5)	-0.0007(5)	-0.0005(4)	-0.0002(5)	-0.0004(5)	-0.0003(4)
O (18e)	$g(O)$	1.00	1.00	1.00	1.00	0.998	0.995	0.991	0.988	0.984	0.980	0.977
	$3-\delta$	3.00	3.00	3.00	3.00	2.994	2.985	2.973	2.964	2.952	2.940	2.931
	$x(O)$	0.4496(4)	0.4516(4)	0.4534(4)	0.4552(4)	0.4574(4)	0.4598(4)	0.4624(4)	0.4651(3)	0.4683(3)	0.4715(3)	0.4742(3)
	$U_{11}, U_{22} (\text{\AA}^2)$	0.0058(3)	0.0062(4)	0.0071(3)	0.0073(4)	0.0069(3)	0.0063(3)	0.0061(2)	0.0066(3)	0.0066(4)	0.0066(3)	0.0064(4)
	$U_{33} (\text{\AA}^2)$	0.0064(3)	0.0078(3)	0.0080(3)	0.0079(4)	0.0077(3)	0.0074(3)	0.0068(3)	0.0072(3)	0.0072(4)	0.0072(3)	0.0075(4)
	$U_{12} (\text{\AA}^2)$	0.0022(10)	0.0022(10)	0.0026(10)	0.0017(10)	0.0019(10)	0.0012(10)	0.0012(9)	0.0018(10)	0.0017(10)	0.0019(10)	0.0019(10)
	$U_{13} U_{23} (\text{\AA}^2)$	-0.0059(8)	-0.0056(8)	-0.0055(8)	-0.0058(8)	-0.0057(8)	-0.0064(8)	-0.0064(8)	-0.0062(7)	-0.0056(8)	-0.0057(8)	-0.0049(7)
Lattice parameters	$x = 0$	$x = 0.05$	$x = 0.10$	$x = 0.15$	$x = 0.20$	$x = 0.25$	$x = 0.30$	$x = 0.35$	$x = 0.40$	$x = 0.45$	$x = 0.50$	
$a, b$ -axis ( $\text{\AA}$ )	5.44110(4)	5.44657(4)	5.44795(4)	5.44850(4)	5.44731(3)	5.44511(4)	5.44208(4)	5.43550(5)	5.43576(5)	5.43173(4)	5.42491(2)	
$c$ -axis ( $\text{\AA}$ )	13.08837(7)	13.11980(8)	13.14057(7)	13.15758(6)	13.17271(6)	13.18596(6)	13.19695(6)	13.19934(8)	13.21706(8)	13.22491(7)	13.22622(7)	
$r_{\text{Co-O}}$ ( $\text{\AA}$ )	1.9318(3)	1.9331(3)	1.9331(3)	1.9328(3)	1.9318(3)	1.9303(3)	1.9285(3)	1.9256(3)	1.9248(3)	1.9228(3)	1.9201(3)	
Co-O-Co ( $^\circ$ )	164.040(7)	164.671(7)	165.286(7)	165.355(7)	166.785(7)	167.543(7)	168.050(7)	168.487(7)	170.689(7)	171.006(7)	171.636(7)	
$R_{\text{wp}}$ (%)	5.353	4.386	4.326	3.920	3.709	3.763	3.684	4.175	4.038	3.552	3.961	
$S$	1.4192	1.1751	1.0646	0.9883	1.0014	0.9855	1.0335	1.1297	1.1474	1.0617	1.2010	
$R_{\text{B}}$ (%)	0.929	1.050	1.389	1.432	1.209	1.356	1.356	1.281	1.268	1.345	1.507	

Note:  $U_{11}, U_{22}, U_{33}, U_{12}, U_{13}$ , and  $U_{23}$ : the atomic anisotropic displacement parameter  $R_{\text{wp}}$  : the reliability weighted pattern factors,  $S$  : the goodness of fit factors ( $= R_{\text{wp}}/R_e$ ,  $R_e$ : the reliability expected factor),  $R_{\text{B}}$  : the reliability Bragg factor.

Table S5 Reliability factor and full width at half maximum of  $(|F_{\text{MEM}}| - |F_{\text{obs}}|)/\sigma_{\text{obs}}$  of Maximum Entropy Method analysis

Parameters	x = 0.00	x = 0.05	x = 0.10	x = 0.15	x = 0.20	x = 0.25	x = 0.30	x = 0.35	x = 0.40	x = 0.45	x = 0.50
$R_w$ (%)	1.2475	1.2139	1.0458	1.3795	1.4092	1.4400	1.3513	1.4799	1.4039	1.3599	1.4070
FWHM of $( F_{\text{MEM}}  -  F_{\text{obs}} )/\sigma_{\text{obs}}$	0.646549	0.550178	0.660847	0.394815	0.625231	0.714376	0.502304	0.660986	0.632016	0.646843	0.778402

Note:  $R_w$  : reliability structure factor of MEM analysis, FWHM : full width at half maximum,  $|F_{\text{MEM}}|$  : structure factor calculated by MEM analysis,  $|F_{\text{obs}}|$  : observed structure factors,  $\sigma_{\text{obs}}$  : estimated standard deviations of observed structure factor.