Experimental details

Growth procedure:

The single crystal of NHO was grown using a traveling floating zone furnace technique starting from a polycrystalline NHO sintered rod. Because of the high melting point of NHO, a furnace equipped with high-performance Xenon lamps was necessary. The polycrystalline NHO source powders for the floating zone growth were synthesized by a calcination of HfO₂ (Alfa-Aesar, 99.9 %) and Nd(OH)₃. Nd(OH)₃ was prepared by soaking Nd₂O₃ (Alfa-Aesar, 99.9 %) powder in distilled water. The resulting Nd(OH)₃ was dried at 60 °C overnight. Before using the Nd(OH)₃ powders, phase purity was assured by X-ray powder diffraction (XRD). Subsequently, a 1:1 stoichiometric mixture of Nd(OH)₃ and HfO₂ powders was ground in an agate mortar, loaded into an alumina crucible and calcinated at 1500 °C for 48 hours. Grinding and calcination were repeated until a phase pure NHO powder was obtained. For the floating zone crystal growth the powder was isostatically pressed to a rod (diameter \sim 8 mm) and sintered at 1500 °C. the floating zone growth was carried out in a 8 bar oxygen atmosphere, further details can be found in Ref. 1.

Measurement details:

XRD powder diffraction patterns were collected on a STOE Stadi P and a Bruker D8-Advance diffractometer using $CuK_{\alpha 1}$ radiation in both of the polycrystalline source powder and the crushed NHO single crystal which shown in fig.1.

The single crystal was sliced to thin plate (thickness ~ 0.3 mm) for the thermal expansion measurement and the capacitance measurement. The thermal expansion coefficient measurement was performed by using a Wien-type micro-dilatometer mounted into a physical properties measurement system (PPMS, Quantum Design). The dielectric properties were measured versus temperature and frequency by capacitance spectroscopy measurements using an Agilent E4980A Precision LCR meter.

 Y. Liu, Z. C. Li, W. P. Liu, G. Friemel, D. S. Inosov, R. E. Dinnebier, Z. J. Li, and C. T. Lin, Supercond. Sci. Technol. 25, 075001 (2012).



Figure S 1: (Color online) XRD patterns of the polycrystalline source powder (upper) and the powder obtained by crushing a small piece of the single crystal $Nd_2Hf_2O_7$ (lower). All the peak positions and their relative intensities are well matched the previous $Nd_2Hf_2O_7$ powder XRD result reported by Ubic *et al.*. Inset : The Enlarged low angle XRD pattern of the single crystal $Nd_2Hf_2O_7$. The weak Bragg peaks indexed as (111) and (311) are characteristic fingerprints of the pyrochlore structure.



Figure S 2: Length change of the single crystal of NHO from 300 K to 2 K. Inset : The linear thermal expansion coefficient of the single crystal.